

Spectral analysis in cosmology

euclid



euclid



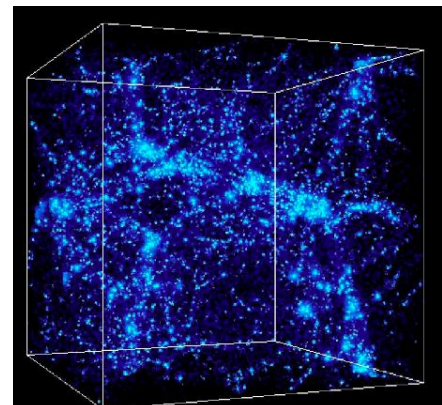
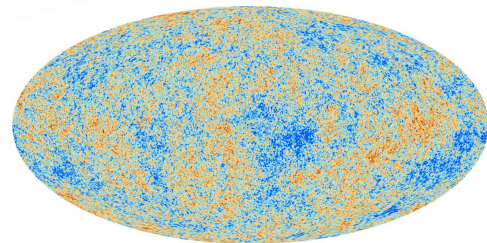
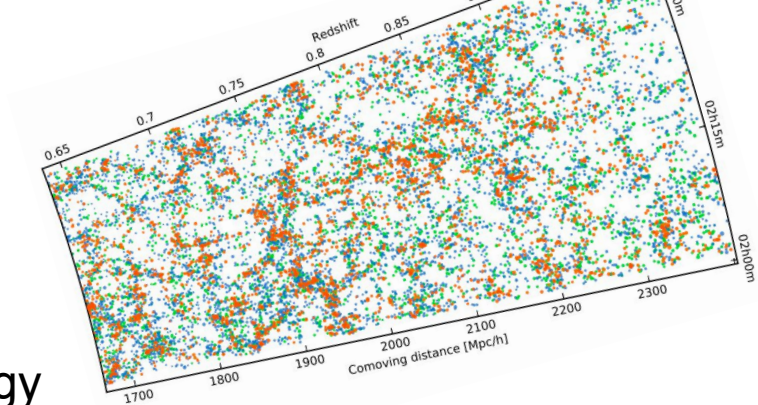
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17 May 2023

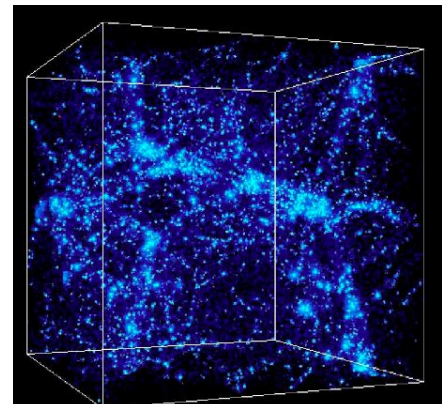
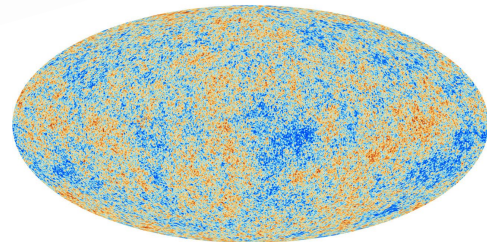
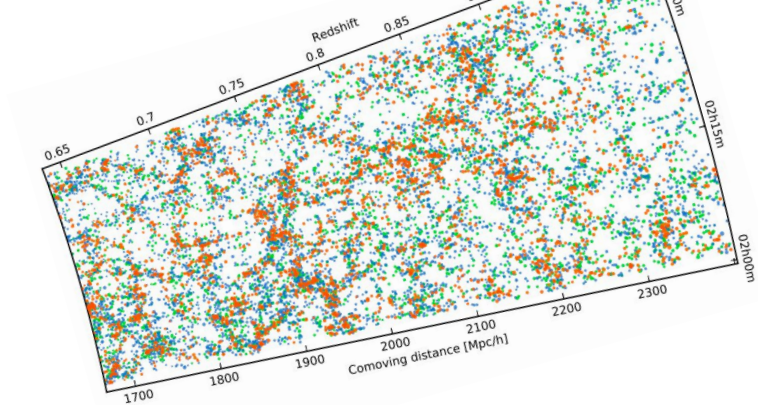
Introduction

- I am a researcher at INAF (Merate)
- My work focuses on observational cosmology with galaxy surveys.
 - [VIPERS](#) (VIMOS Public Extragalactic Redshift Survey)
 - [ESA Euclid](#) space telescope mission
- Previously I analysed cosmic microwave background maps.
- I am also interested in computation and data science.



Contents

- [Euclid](#)
- [Standard model of cosmology](#)
- [Three-dimensional analysis](#)
 - Cosmic web of galaxies
 - Dynamical equations
 - Power spectrum
 - Correlation function
 - Baryon acoustic oscillations
 - Redshift-space distortions



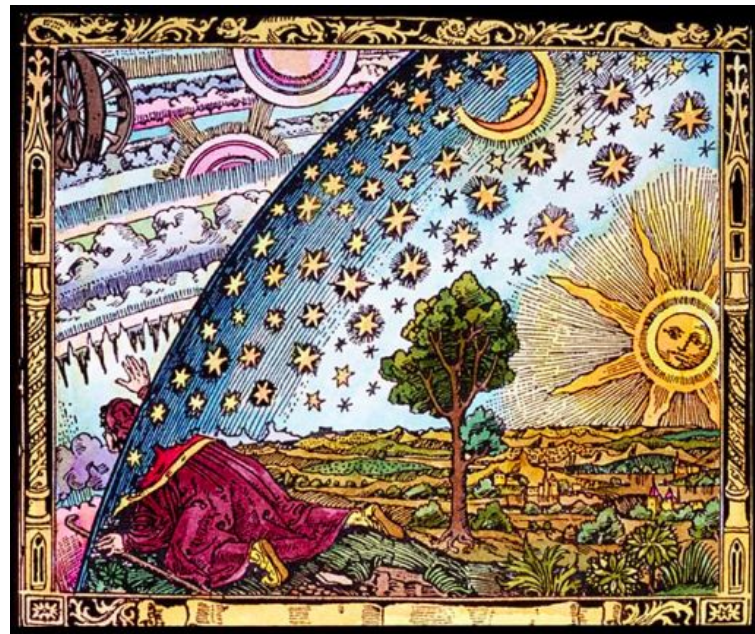
References

Euclid mission

- ESA page: <https://sci.esa.int/web/euclid>
- Red book: <https://arxiv.org/abs/1110.3193>

Cosmology

- Longair, 1998, **Galaxy Formation**
- Peacock, 1998, **Cosmological Physics**
- Dodelson, 2003, **Modern Cosmology**
- Planck results
<https://www.cosmos.esa.int/web/planck/publications>
- Martin White's BAO animation
<http://w.astro.berkeley.edu/~mwhite/bao/>

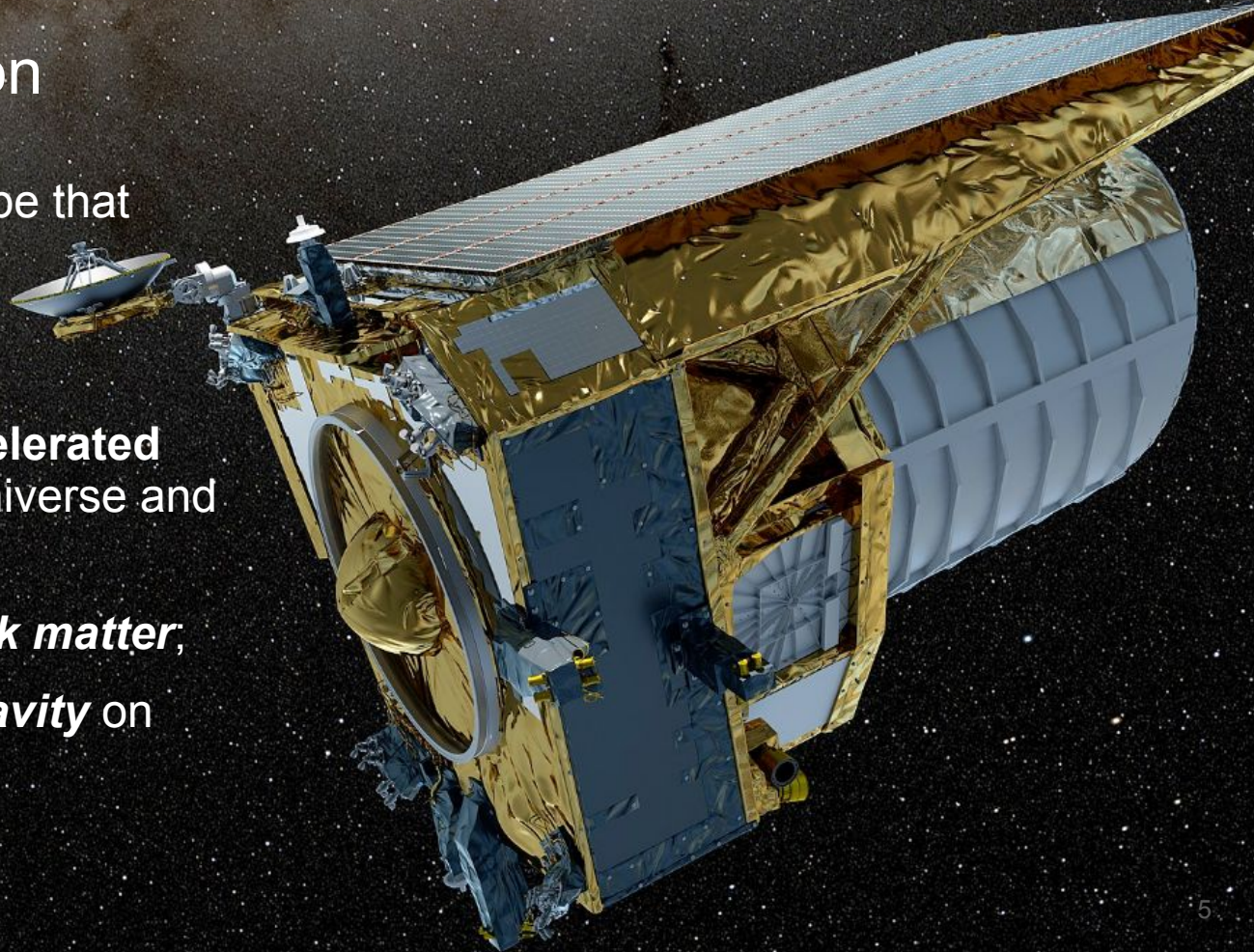


- https://en.wikipedia.org/wiki/Flammarion_engraving
- <https://gallica.bnf.fr/ark:/12148/bpt6k408619m/f168.item>

ESA Euclid mission

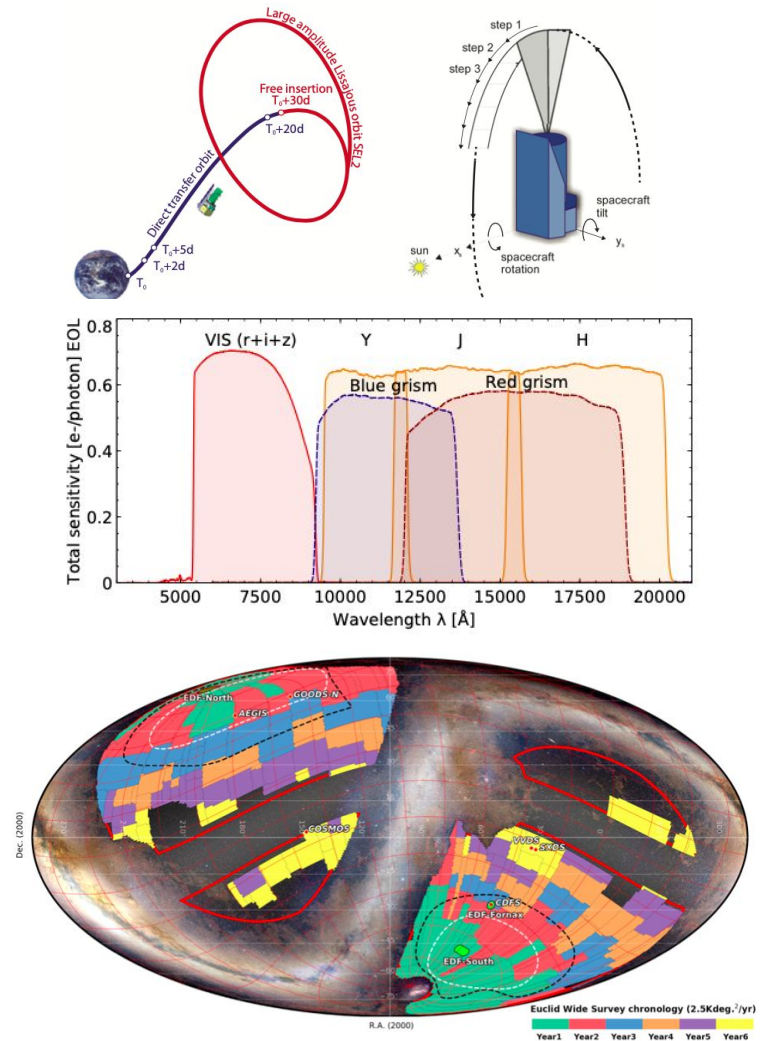
Euclid is a space telescope that will map the visible and *dark* components of the Universe to understand

- the origin of the **accelerated expansion** of the Universe and ***dark energy***,
- the properties of ***dark matter***;
- and the nature of ***gravity*** on cosmological scales.



The Euclid mission

- Euclid is a space telescope that will orbit L2.
- Two instruments will do imaging and spectroscopy.
 - Visible camera (VIS)
 - Near Infrared Spectrometer and Photometer (NISP)
- Two surveys: Wide (15000 sqr deg) and Deep (40 sqr deg)



Euclid cosmological probes

Euclid will measure the effects of **dark energy**, **dark matter** and **gravity** with two complementary observables:

- the expansion history of the Universe,
- and the history of structure formation.

The expansion history will be measured by multiple techniques: the BAO scale measured with galaxy clustering, and weak gravitational lensing.

The history of structure formation will be measured by redshift-space distortions in galaxy clustering, weak gravitational lensing and the galaxy cluster mass function.

Complementary measurements will give a high control on systematic errors.

Euclid legacy science in numbers

| What | Euclid |
|---|--------------------------------------|
| Galaxies at $1 < z < 3$ with good mass estimates and morph. | $\sim 2 \times 10^8$ |
| Massive galaxies ($1 < z < 3$) w/ spectra | $\sim \text{few} \times 10^3$ |
| H α emitters/metal abundance at $z \sim 1-2$ | $\sim 4 \times 10^7 / 10^4$ |
| Galaxies in massive clusters at $z > 1$ | $\sim (2-4) \times 10^4$ |
| Type 2 AGN ($0.7 < z < 2$) | $\sim 10^4$ |
| Galaxy mergers | $\sim 10^5 - \text{few} \times 10^6$ |
| Strongly lensed galaxy-scale lenses | $\sim 300,000$ |
| $z > 8$ QSOs | ~ 30 |

- The unprecedented near-infrared imaging and spectroscopic survey of $\frac{1}{3}$ sky will be the reference catalog for the next decades.

Payload module (PLM)

VIS electronics radiator

VIS focal plane inside hood

VIS shutter

NISP Opto-mechanical
Assembly

Fold Mirror 1

Tertiary Mirror

Fold Mirror 3

VIS Calibration Unit

NISP radiator

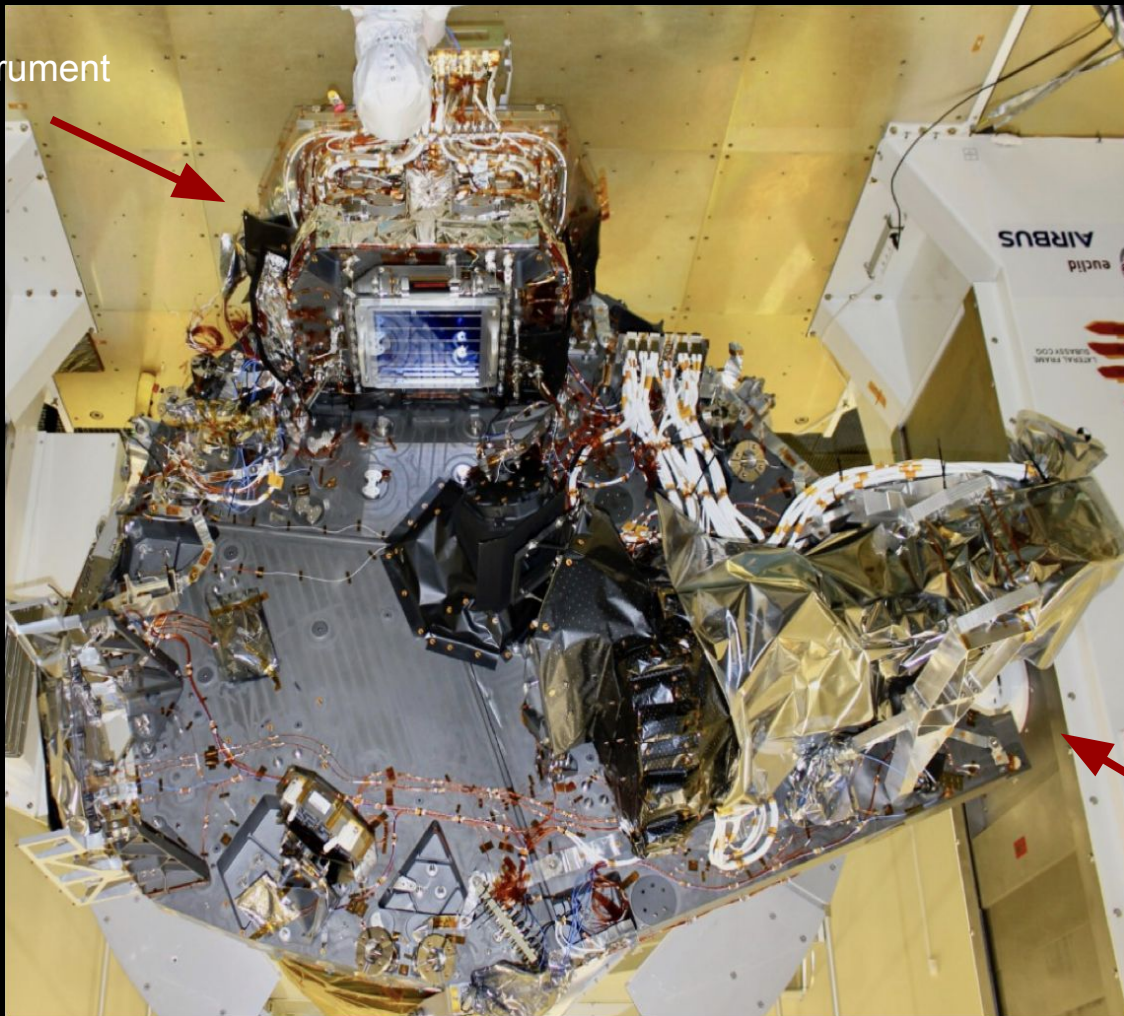
Fold Mirror 2

Dichroic

Telescope (facing downwards)

Payload module (PLM)

VIS instrument



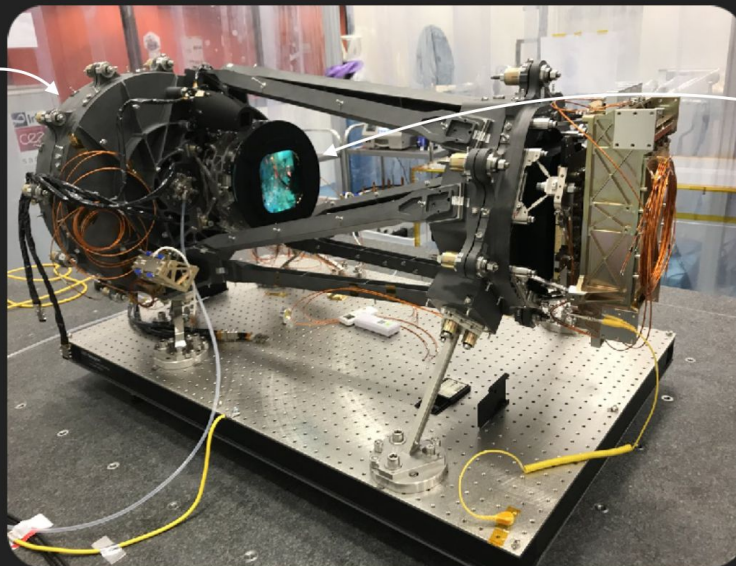
NISP
instrument

Euclid NISP instrument

Slides courtesy William Gillard



CoLA (Corrector lens Assembly)



CaLA (Camera lens Assembly)



Slitless Spectrometer:

RGS 0°, 180°, 270° 1250-1850 nm

BGS 0° 920-1250 nm

Photometer:

FW-Y 950 - 1192 nm

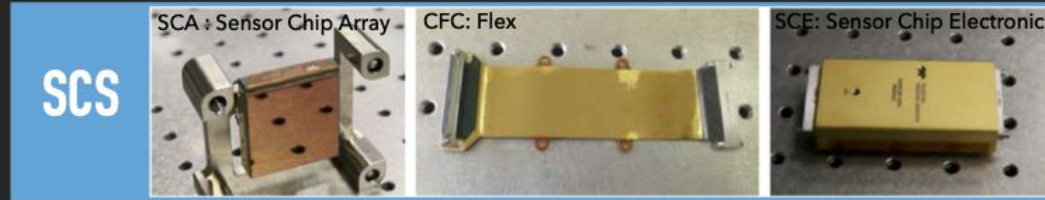
FW-J 1192 - 1544 nm

FW-H 1544 - 2000 nm



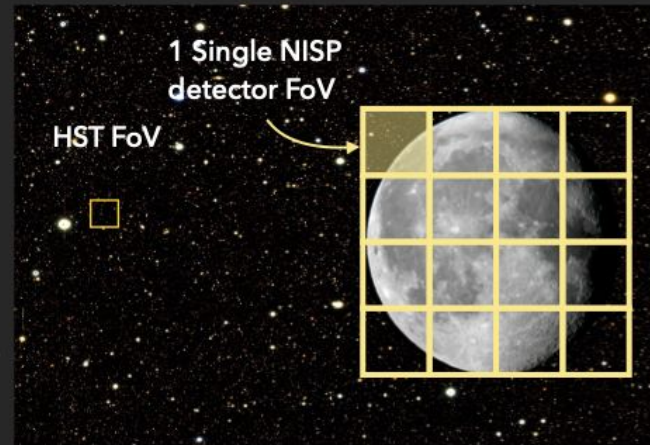
THE NEAR INFRARED FOCAL PLANE

Focal plane comprises 16 near-IR detectors called SCS (Sensor Chip Sys.)

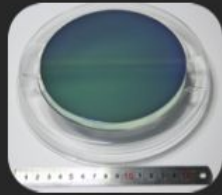


1 SCA = Array of $2k \times 2k$ pixels of $18 \mu m$ each $\Rightarrow 0.3''$ / pix

field-of-view of
 $0.53^\circ \times 0.53^\circ$



Few thousands of galaxies in a single pointing



NISP FM Grism

4 Grism :

BGS000
920 -1350 nm

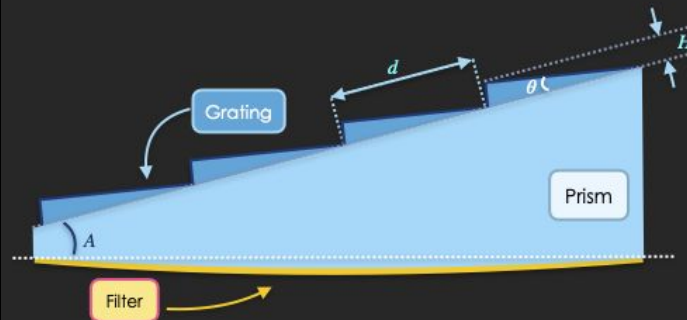
RGS000
1250-1850 nm

RGS180
1250-1850 nm

RGS270
1250-1850 nm

Spectrometric redshift measurement for :

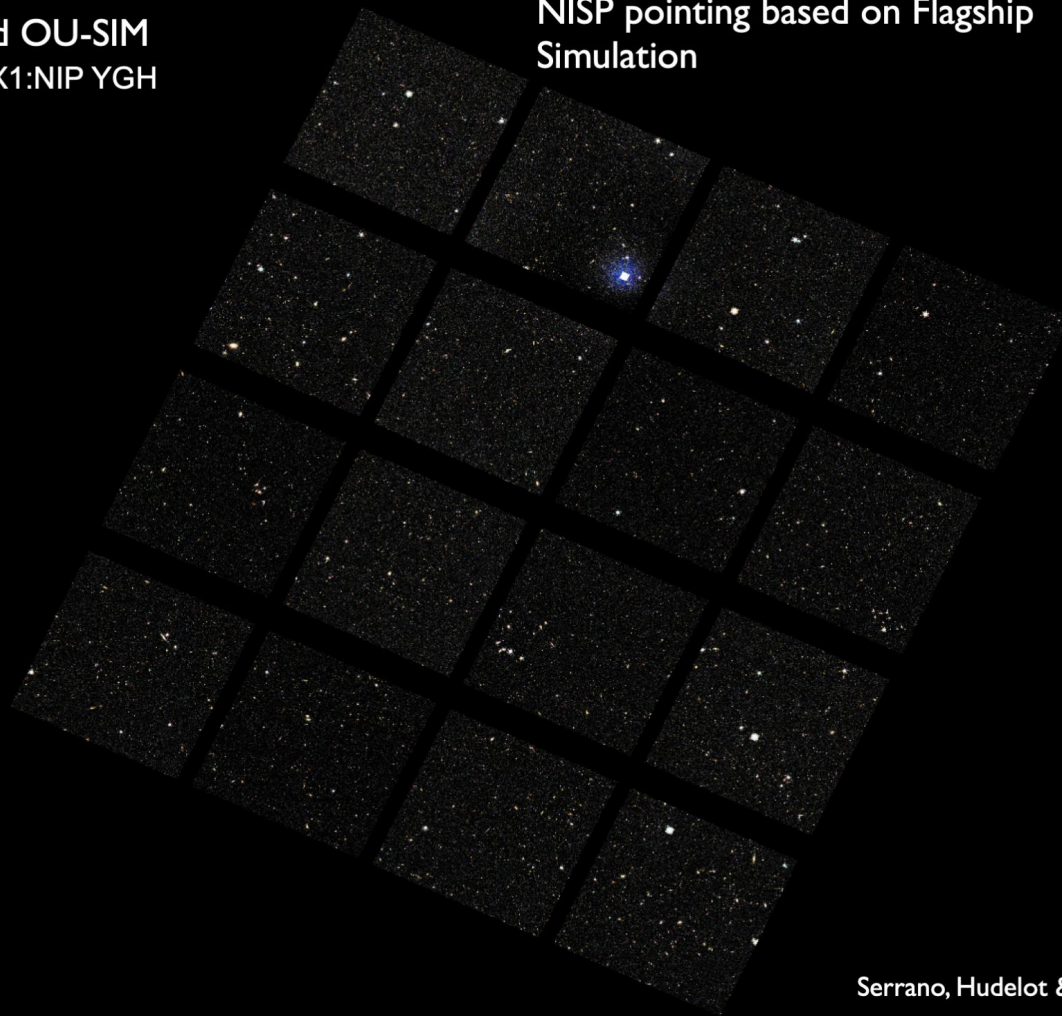
- H α line between $0.4 < z < 1.8$
- O $_{III}$ line between $0.8 < z < 2.7$



- The **Grating** : disperse light and provide image spectra
- The **Prism** : compensate for the light deviation induced by the grating allowing to images spectrum onto the NISP focal plane.
- The **Filter** : select bandpass → **convex surface to focalise light onto the detectors**

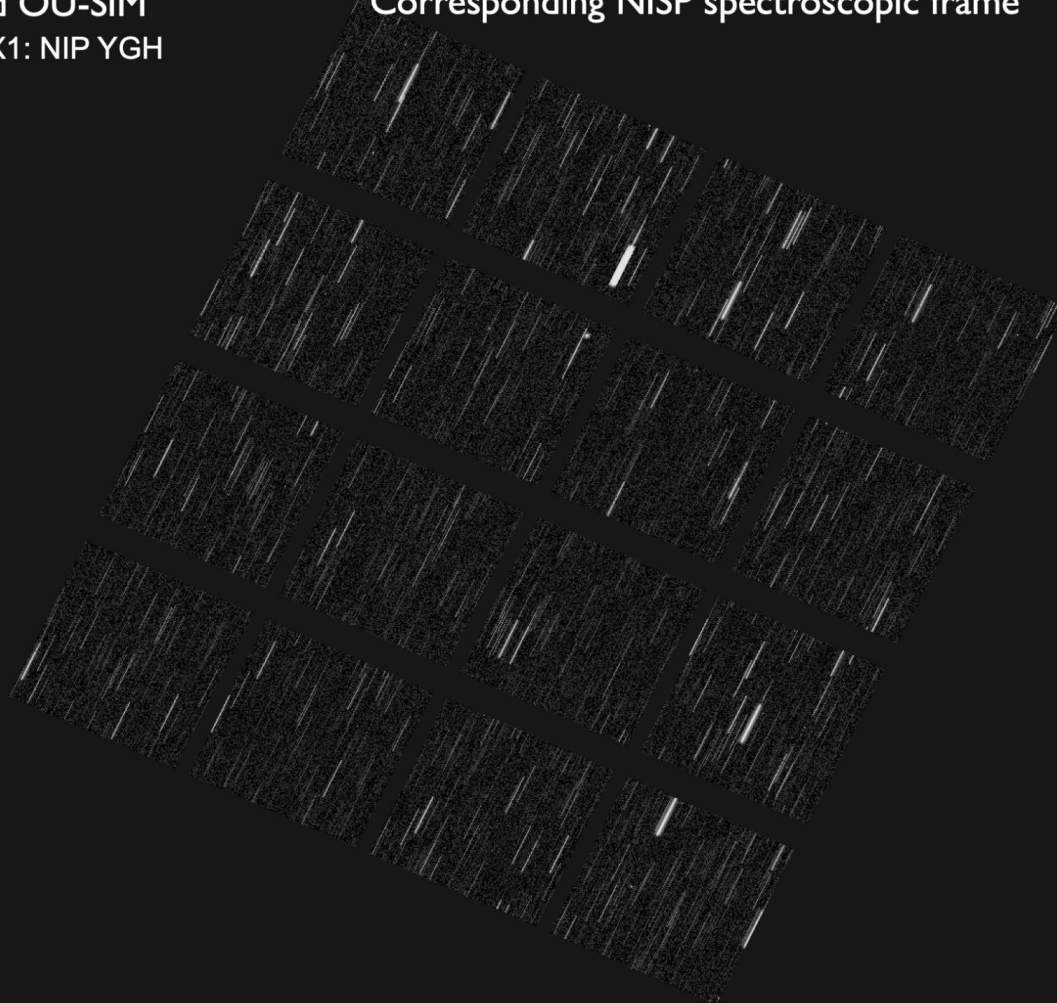
Euclid OU-SIM
Field X1:NIP YGH

NISP pointing based on Flagship
Simulation



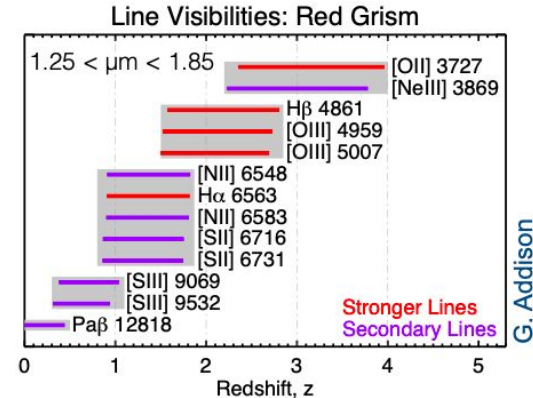
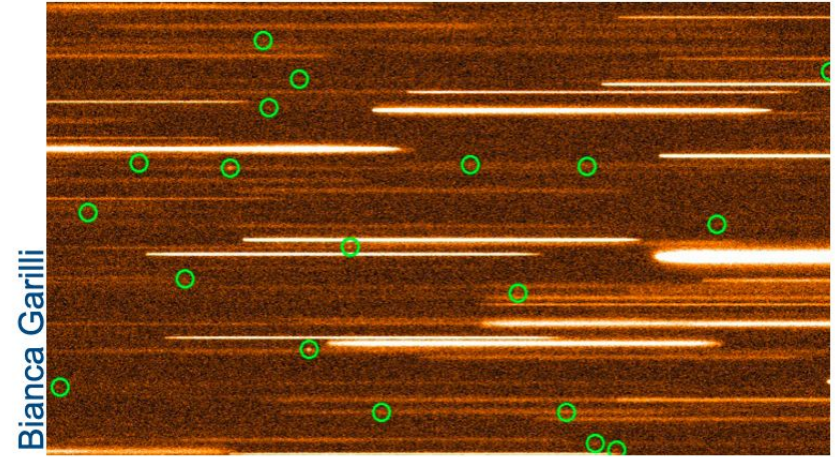
Euclid OU-SIM
Field X1: NIP YGH

Corresponding NISP spectroscopic frame



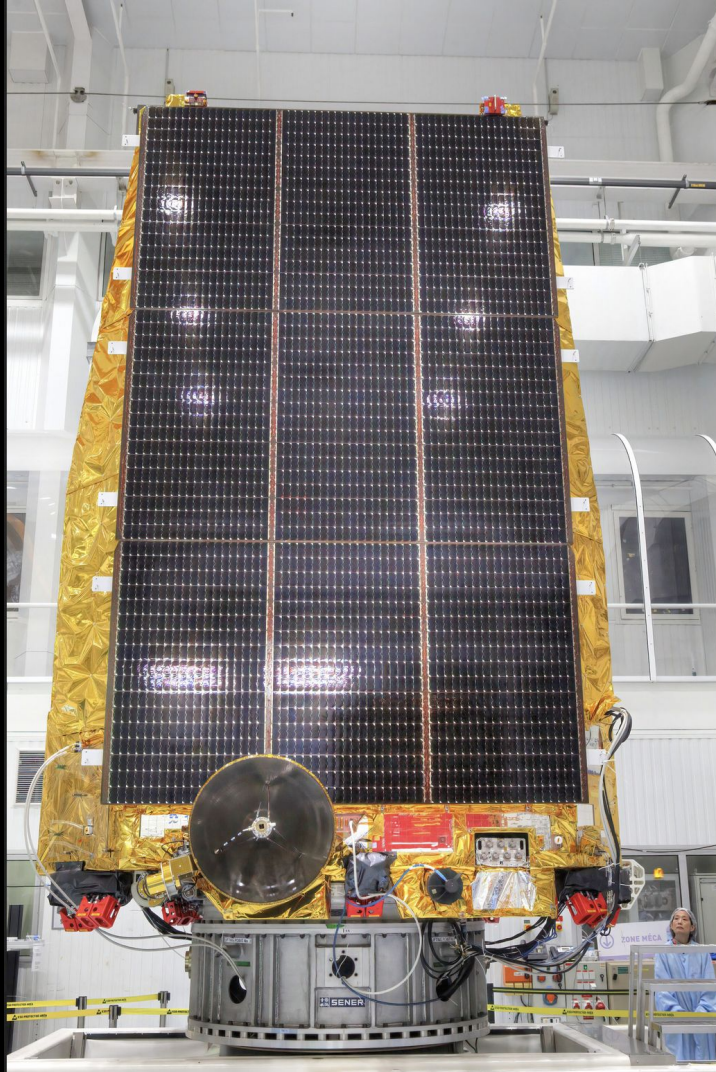
Euclid NISP redshift survey

- Euclid will measure galaxy redshifts from emission lines detected in slitless spectroscopy
- Primarily emission line H α in $0.9 < z < 1.8$



Euclid

Final assembly at
Thales in Cannes.



ESA's Euclid mission @ESA_Euclid · 14 apr
While @ESA_JUICE is waiting at @EuropeSpacePort for good sky to fly today to space, @ESA_Euclid after road transport from Cannes (France) to Savona (Italy) is now ready to sail to Cape Canaveral in a dedicated container on the #MNColibri ship.



3 50 127 17.782

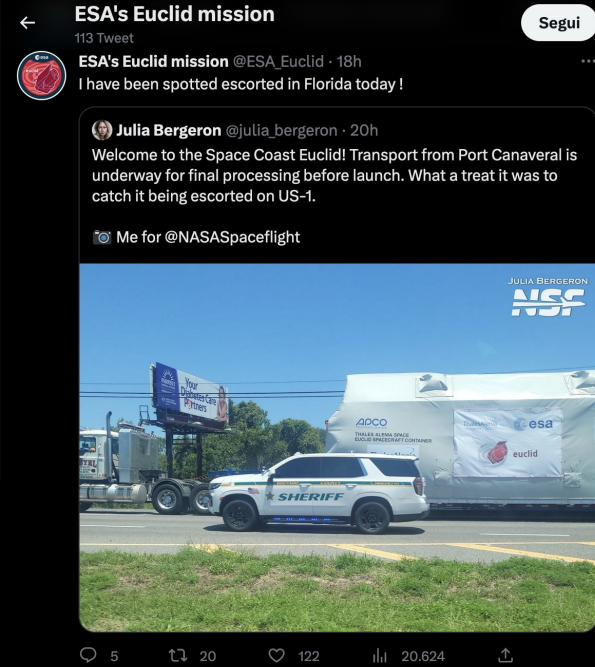
14 April



15 April

Euclid travels from Cannes to Savona
to Florida's Cape Canaveral

https://twitter.com/ESA_Euclid

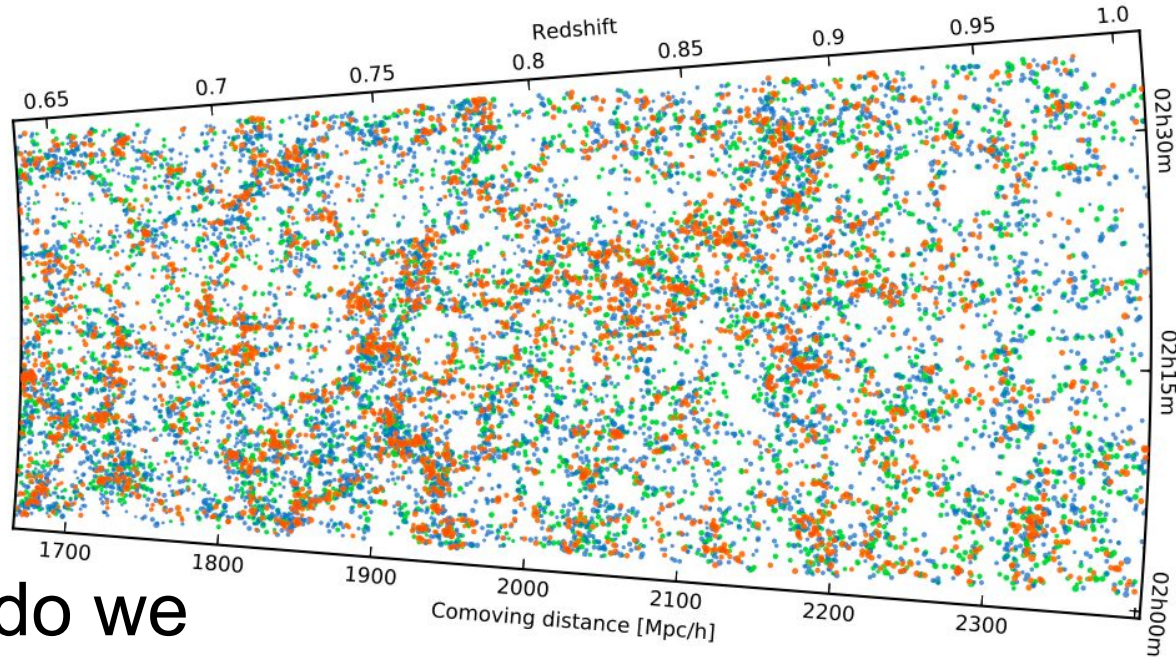


1 May

Euclid will launch on a
Falcon 9 rocket in July



Now, get ready for the data flood!



But, how do we
get cosmology
out?

2. Standard model of cosmology

- The *flat lambda cold dark matter* (Λ CDM) model is established as the standard model in cosmology.
- The dynamics of the Universe on large scales are governed by general relativity.
- Observational evidence indicates that the geometry is *flat*.
- Separations are measured with the Friedmann-Lemaître-Robertson-Walker metric

$$ds^2 = a(t)^2 (dx^2 + dy^2 + dz^2) - c^2 dt^2$$

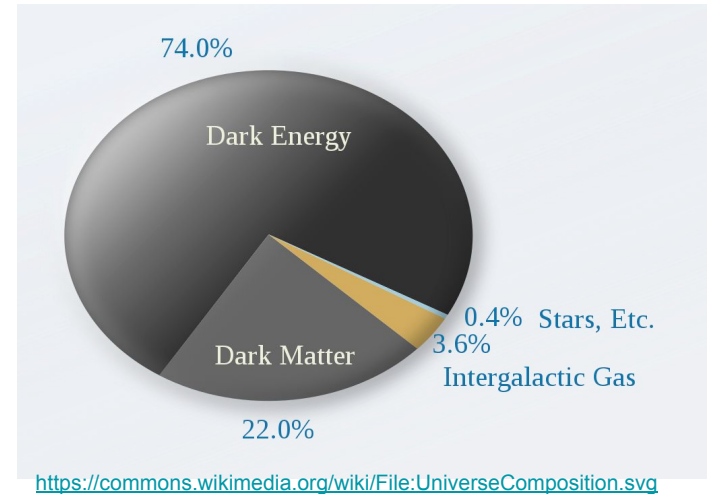
- The scale factor $a(t)$ characterises the expansion of the Universe
 $a=1$ today, $a<1$ in the past.

Components of the Universe

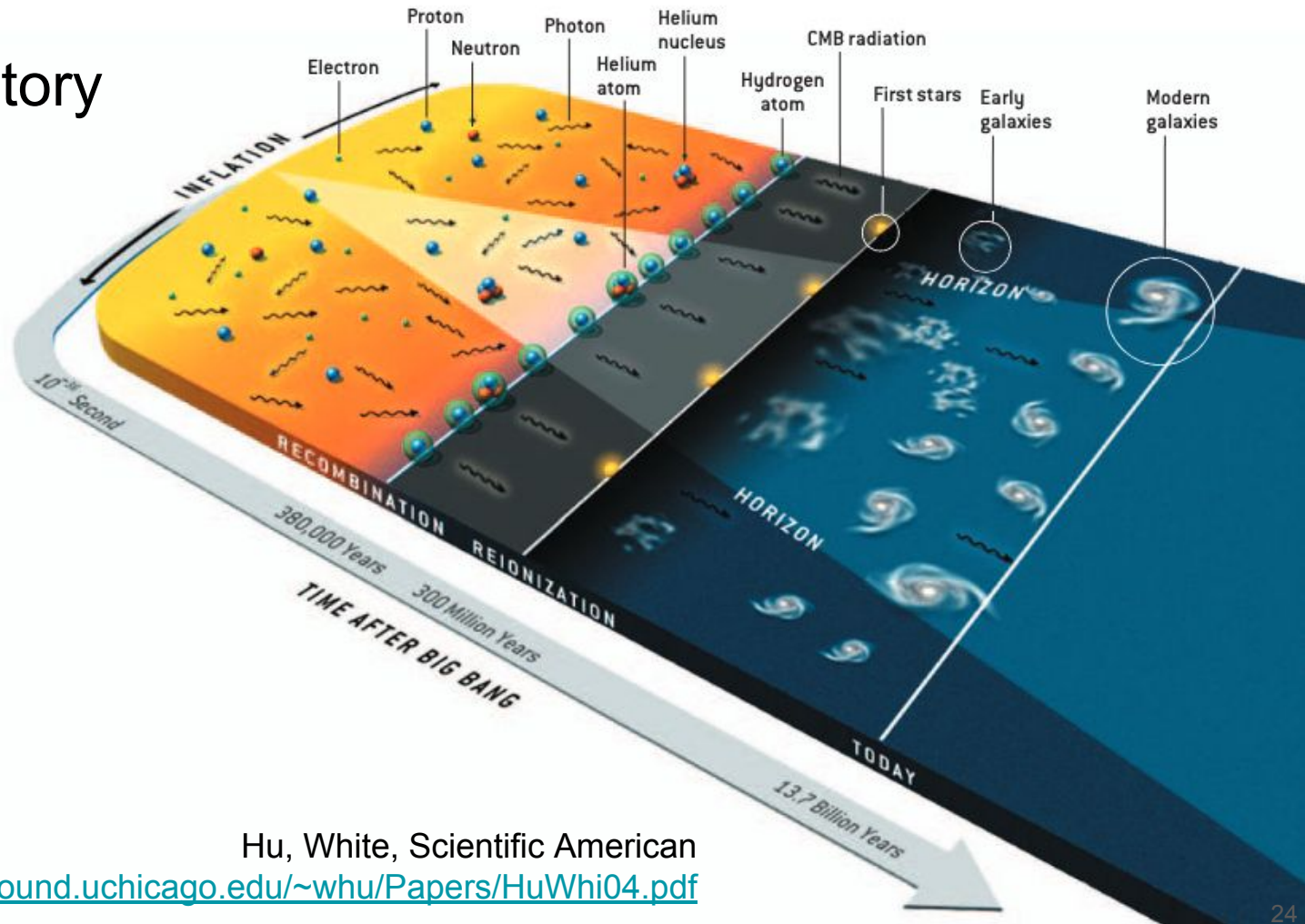
- The Universe is made up of:
 - **baryons** ~4.56% of total energy density
 - **photons** ~0.00498%
 - **neutrinos** ~0.00339%
 - **dark matter** ~22.7%
 - **dark energy** ~72.8%

(Planck 2018 paper, <https://www.cosmos.esa.int/web/planck/publications>)

- **Dark matter** and **dark energy** are modeled as fluids.
 - We can measure the equations of state but their physical identities are unknown.



Thermal history



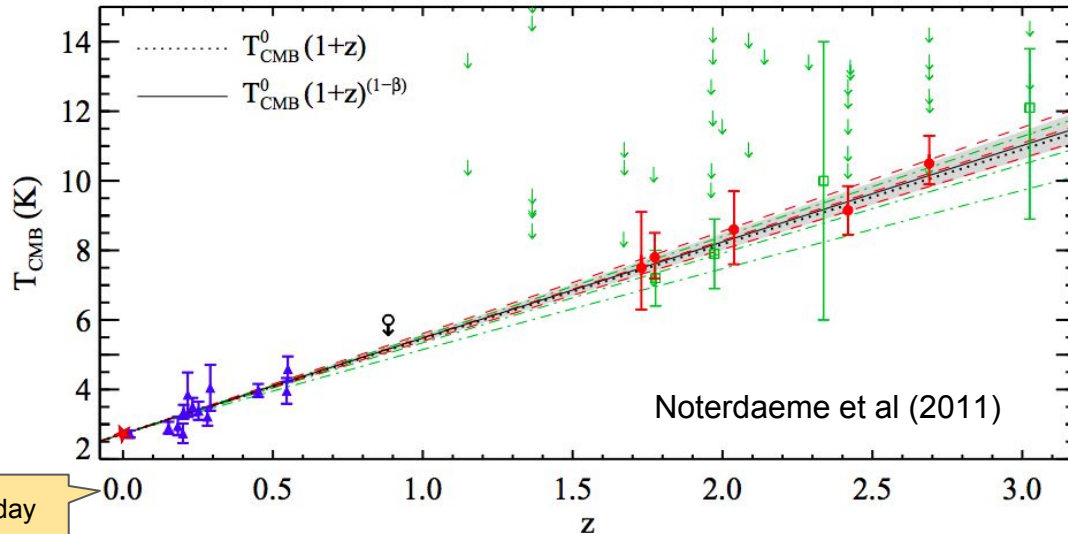
Hu, White, Scientific American

<http://background.uchicago.edu/~whu/Papers/HuWhi04.pdf>

Thermal history

- The temperature of black body radiation cools as $T \sim 1/a$ therefore, the Universe was hotter in the past.
- Extrapolating back to a singularity we reach the *Big Bang*.

P. Noterdaeme et al.: The evolution of the Cosmic Microwave Background Temperature

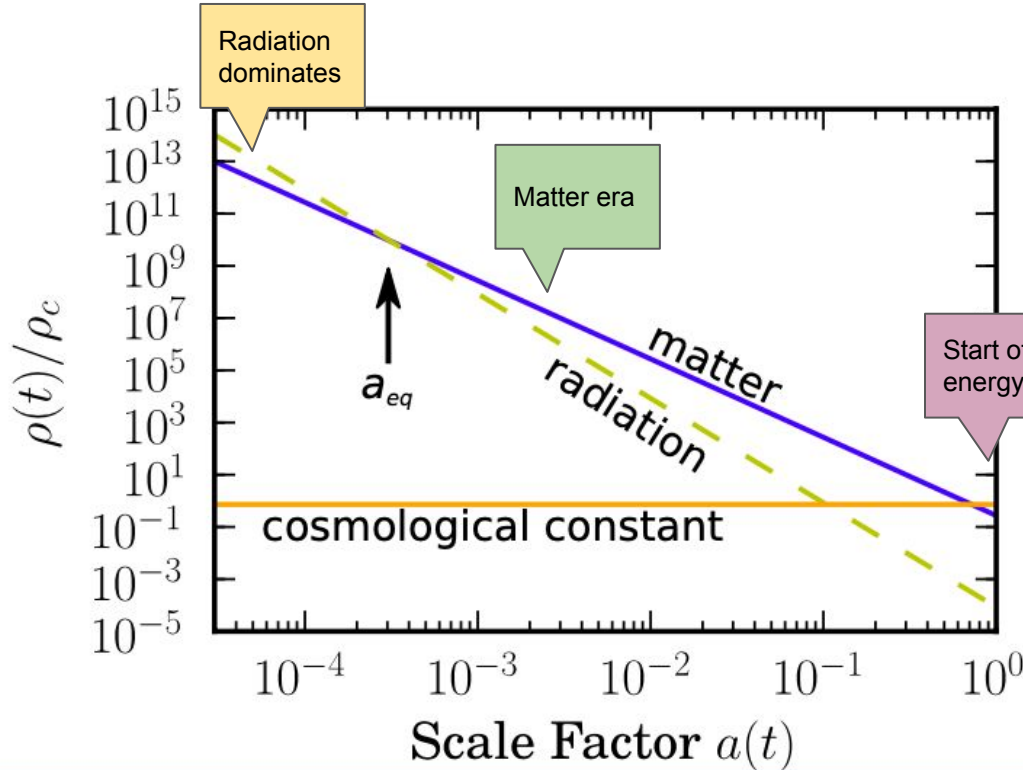


The **cosmic microwave background (CMB)** radiation is a near perfect black body. The temperature can be tracked backward in cosmic time.

Today $T=2.725$ K (COBE satellite)

(Redshift is defined $z = 1/a - 1$
 $z=0$ today)

Thermal history



- The dependence of the density on scale factor varies with the equation of state of the material

$$w = Q/P$$

- Dark energy is modeled with the cosmological constant

| Component | evolution | w | ρ_0/ρ_c |
|-------------|--|-----|----------------------|
| dark matter | $\rho_{cdm} = \rho_{cdm,0} a^{-3}$ | 0 | 0.227 ± 0.014^a |
| baryons | $\rho_b = \rho_{b,0} a^{-3}$ | 0 | $0.0456 \pm .0016^a$ |
| radiation | $\rho_\gamma = \rho_{\gamma,0} a^{-4}$ | 1/3 | $4.98 \cdot 10^{-5}$ |
| neutrinos | $\rho_\nu = \rho_{\nu,0} a^{-4}$ | 1/3 | $3.39 \cdot 10^{-5}$ |
| dark energy | $\rho_\Lambda = \text{constant}$ | -1 | $0.728 \pm .0015^a$ |

^a WMAP+BAO+H0 best-fit parameters

The Early Universe

- The young universe is filled with a hot plasma.
 - Photons and baryons in equilibrium.

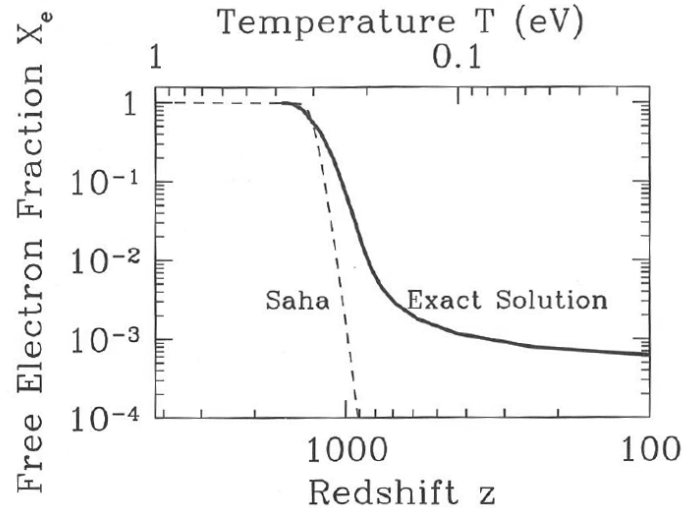


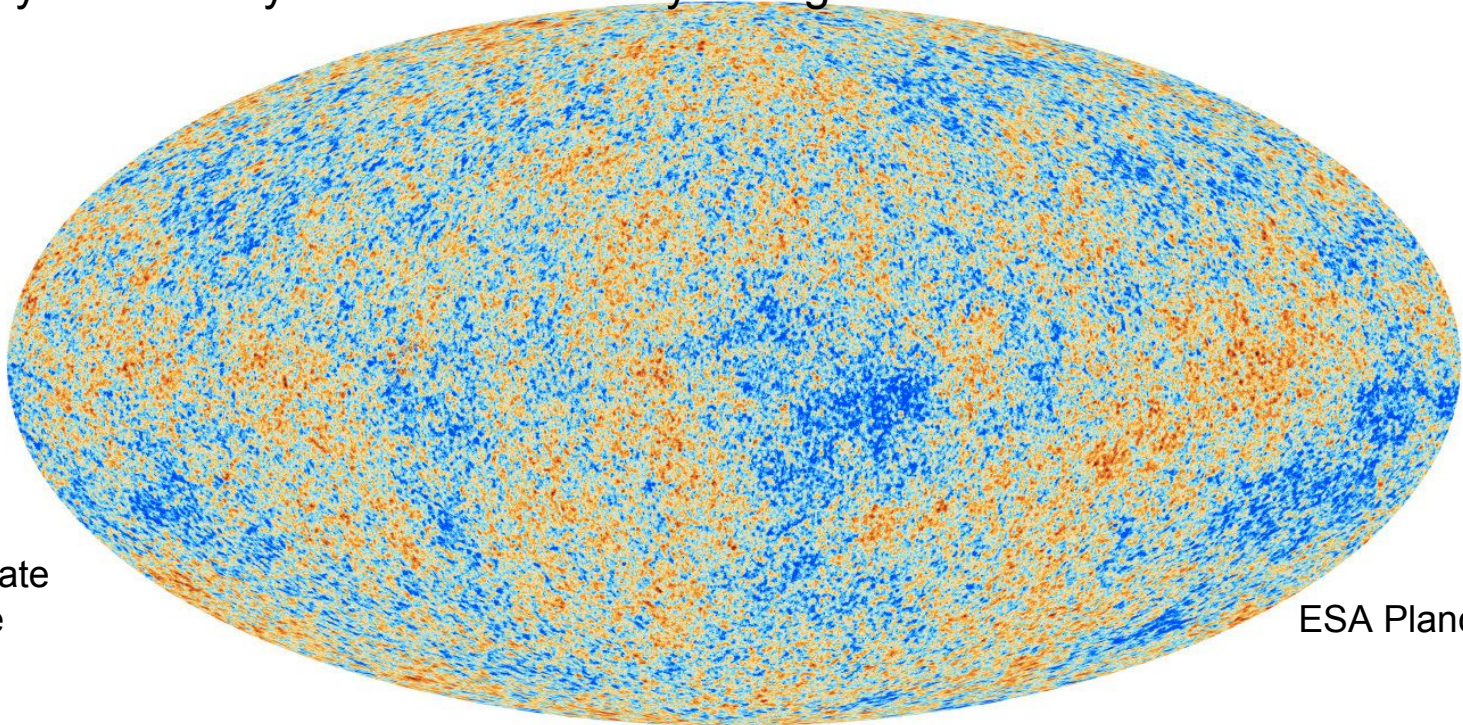
Figure 3.4. Free electron fraction as a function of redshift. Recombination takes place suddenly at $z \sim 1000$ corresponding to $T \sim 1/4$ eV. The Saha approximation, Eq. (3.37), holds in equilibrium and correctly identifies the redshift of recombination, but not the detailed evolution of X_e . Here $\Omega_b = 0.06$, $\Omega_m = 1$, $h = 0.5$.

Dodelson, 2003, *Modern Cosmology*

- Ends at **recombination** ($z \sim 1000$, $t \sim 10^5$ years)
 - The temperature drops to 1/4 eV allowing neutral hydrogen to exist.
 - The **mean free path** of photons becomes large and Universe becomes transparent.
 - These photons are observed today as the cosmic microwave background radiation.

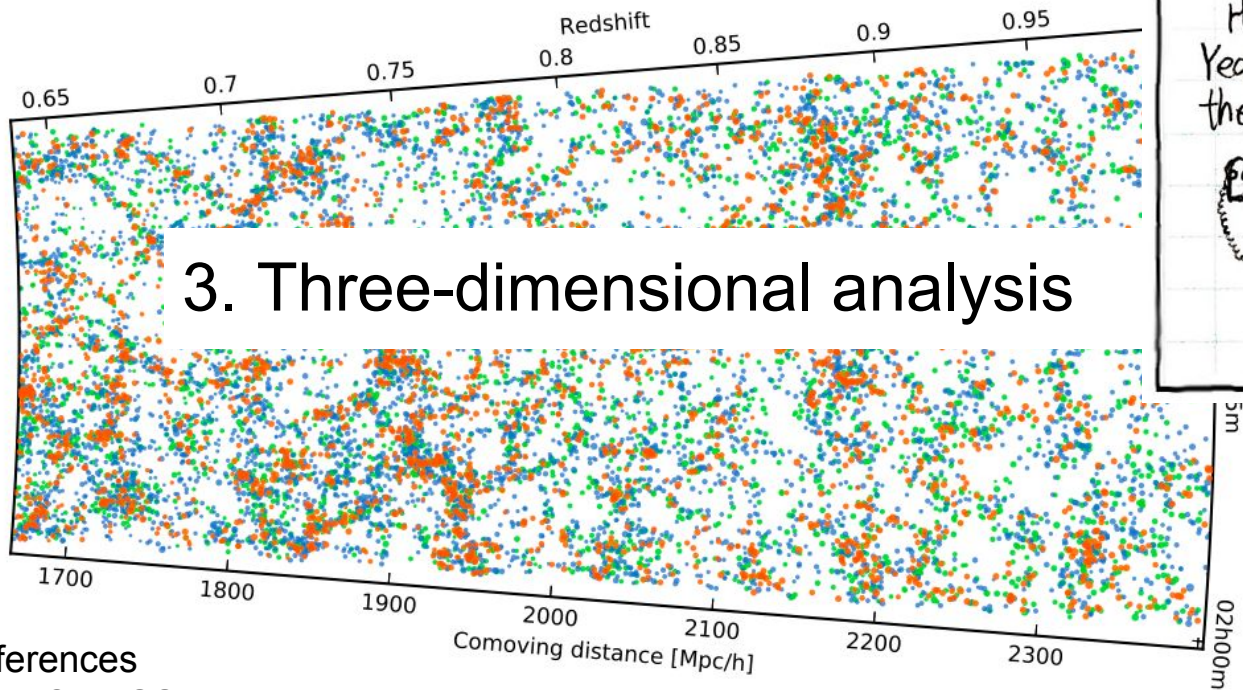
Cosmic microwave background radiation (CMBR)

- The radiation field is mostly unmodified after recombination and we see it today as a nearly uniform blackbody background with $T=2.7\text{ K}$

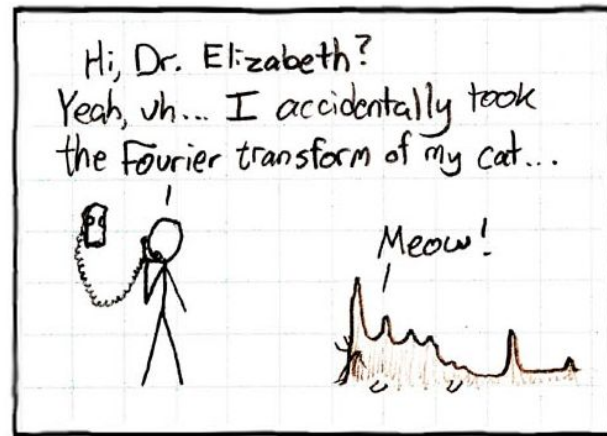


Colors indicate
temperature
 $\Delta T/T \sim 10^{-5}$

ESA Planck



3. Three-dimensional analysis



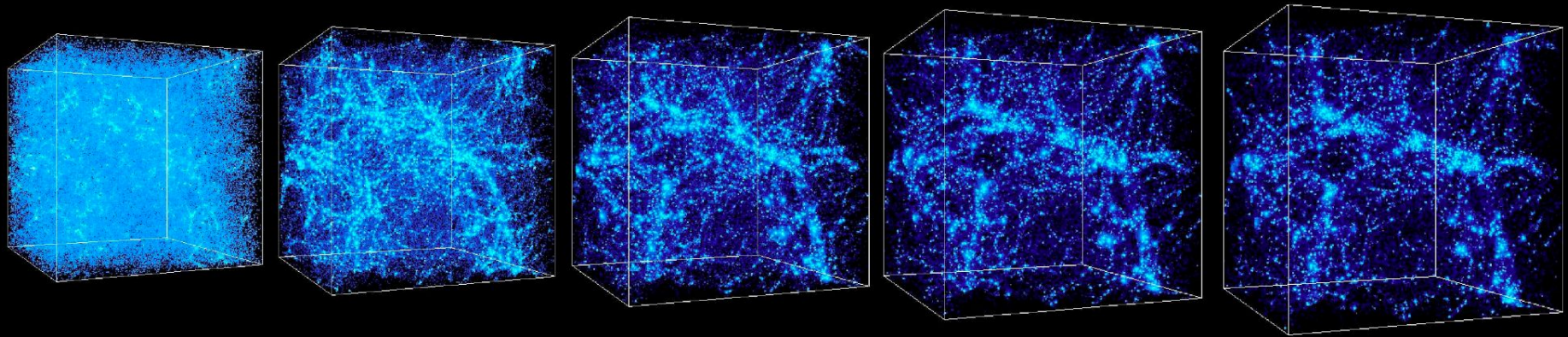
kxcd.com/26

References

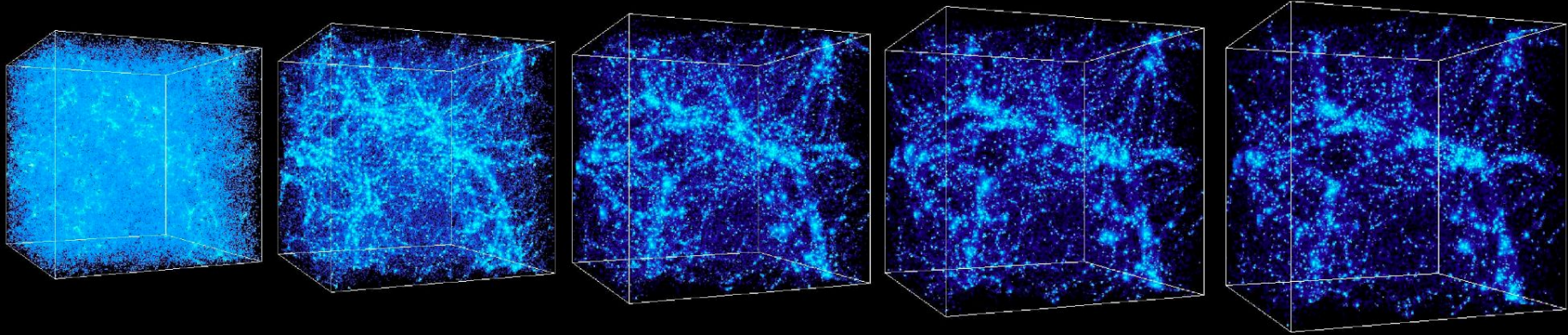
- **CMASS results** http://www.sdss3.org/science/boss_publications.php
- **VIPERS results** <http://vipers.inaf.it>
- Rota+2017, **VIPERS galaxy power spectrum** <https://arxiv.org/abs/1611.07044>
- Granett+2015, **VIPERS maximum likelihood reconstruction** <https://arxiv.org/abs/1505.06337>
- Peacock, 1998, **Cosmological Physics**
- Longair, 1998, **Galaxy Formation**

Formation of the cosmic web

- The cosmic web forms through gravitational collapse from homogeneous initial conditions.
- Define the overdensity of matter with respect to the mean density: $\delta = \frac{\rho - \bar{\rho}}{\bar{\rho}}$
- Jeans instability: largest density perturbations collapse first.
- Small perturbations $\delta \ll 1$ grow linearly according to the growth factor: $\delta(z) = \delta(0)D(z)$



Why spectral analysis?



- Fourier analysis is fundamental to gain physical insight and solve the dynamical equations that describe structure formation.

Dynamical equations

- We will start with the differential equations defining the dynamics of a fluid:

Continuity equation: $\frac{D\rho}{Dt} = -\rho \nabla \cdot \vec{v}$

Equation of motion: $\frac{D\vec{v}}{Dt} = -\frac{1}{\rho} \nabla p - \nabla \phi$

Scalar density: ρ

Scalar pressure: p

Vector velocity: \vec{v}

Scalar gravitational potential: ϕ

Poisson equation: $\nabla^2 \phi = 4\pi G \rho$

$$\frac{D}{Dt} = \frac{\partial}{\partial t} + \vec{v}_0 \cdot \nabla$$

Linearized equations

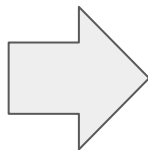
- Linearize the equations by expanding to first order in the perturbations.

$$\vec{v} = \vec{v}_0 + \delta\vec{v}$$

$$\rho = \rho_0 + \delta\rho$$

$$p = p_0 + \delta p$$

$$\phi = \phi_0 + \delta\phi$$

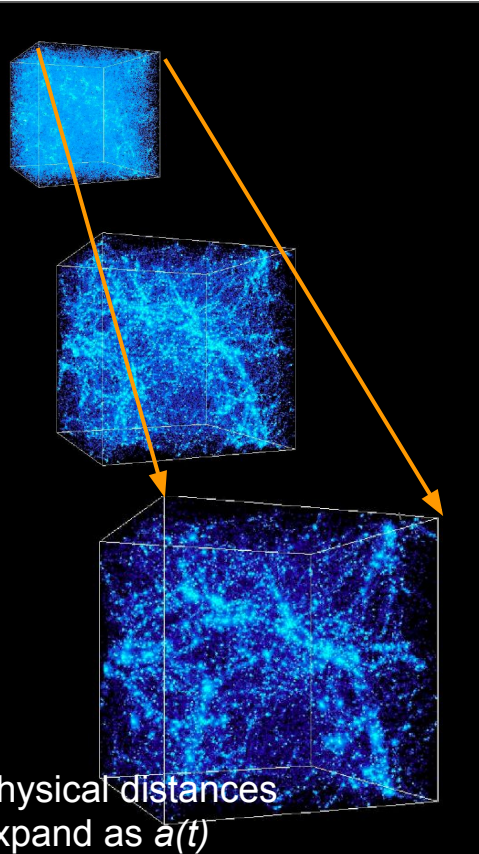


$$\frac{D\delta\vec{v}}{Dt} = -\frac{1}{\rho_0}\nabla\delta p - \nabla\delta\phi - (\delta\vec{v} \cdot \nabla)\vec{v}_0$$

$$\frac{D}{Dt} \left(\frac{\delta\rho}{\rho_0} \right) = -\nabla \cdot \delta\vec{v}$$

$$\nabla^2\delta\phi = 4\pi G\delta\rho$$

Change to coordinates comoving with the Hubble flow



$$\vec{x}(t) = a(t)\vec{r}(t)$$

$$\vec{v} = \frac{d\vec{x}}{dt} = \frac{da}{dt}\vec{r} + a(t)\frac{d\vec{r}}{dt}$$

Hubble expansion

Perturbation

$$= H\vec{x} + \delta\vec{v}$$

$$\delta\vec{v}(t) = a(t)\vec{u}(t)$$

Result

- Linearized differential equations that describe the evolution of the density field.

*Velocity field
(equation of motion)*

$$\frac{d\vec{u}}{dt} + 2\frac{\dot{a}}{a}\vec{u} = \frac{\nabla\delta\phi}{a^2} - \frac{1}{\rho_0}\nabla\delta p$$

*Density field
(continuity equation)*

$$\frac{d\delta}{dt} = -\nabla \cdot \vec{u}$$

Spectral decomposition

- Find the solution for a plane wave:

$$\delta \propto e^{-i\vec{k}\cdot\vec{r}}$$

- Define the sound speed and Jean's length:

$$c_s^2 = \frac{\partial p}{\partial \rho} \qquad \lambda_J = \frac{2\pi}{k_J} = c_s \sqrt{\frac{\pi}{G\rho_0}}$$

- Result:

$$\ddot{\delta} + 2\frac{\dot{a}}{a}\dot{\delta} = \delta \left(4\pi G\rho_0 - \frac{c_s^2 k^2}{a^2} \right)$$

- Large scales, neglect pressure: $\ddot{\delta} + 2\frac{\dot{a}}{a}\dot{\delta} = \delta \left(4\pi G\rho_0 - \frac{c_s^2 k^2}{a^2} \right)$

Power law solutions

- Cold dark matter case, matter dominated with $\Omega=1$:

$$\delta \propto t^{2/3} \propto a = (1+z)^{-1}$$

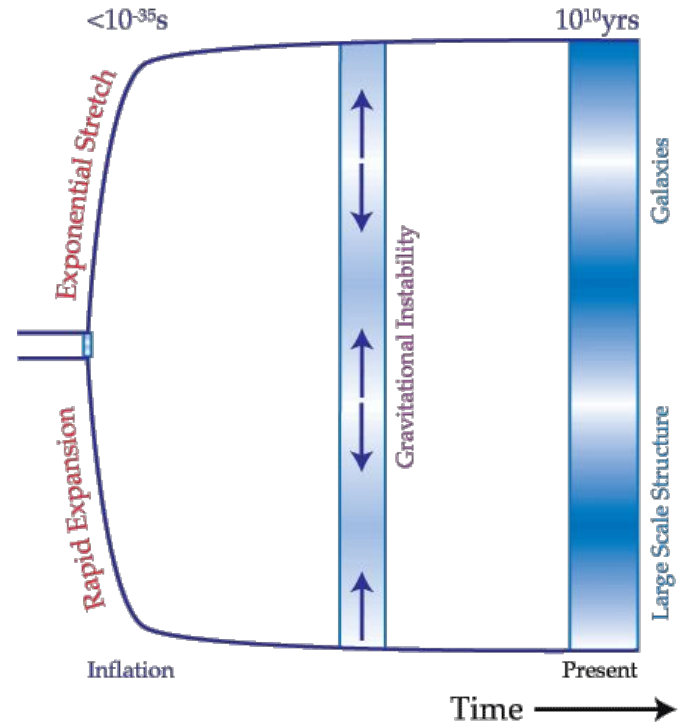
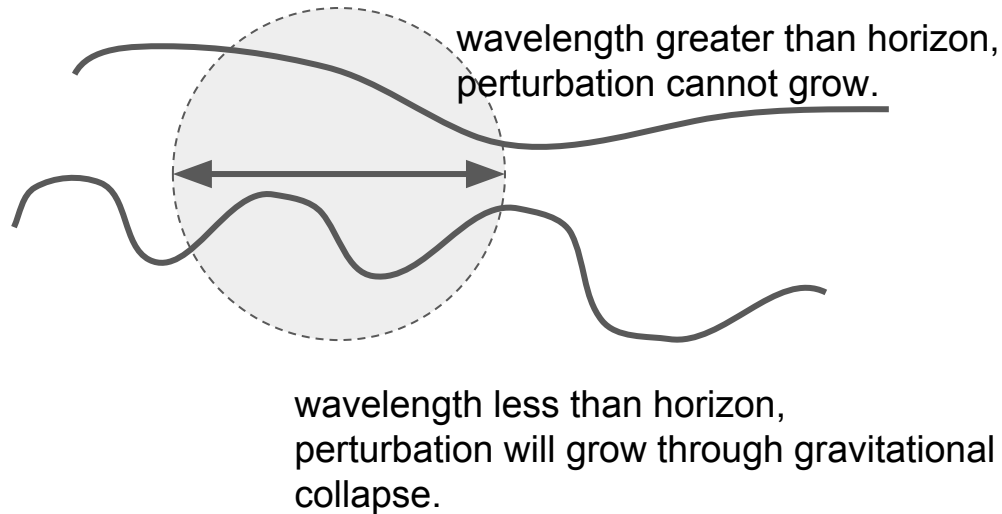
- Radiation case ($\Omega=1$):

$$\delta \propto t \propto a^2 = (1+z)^{-2}$$

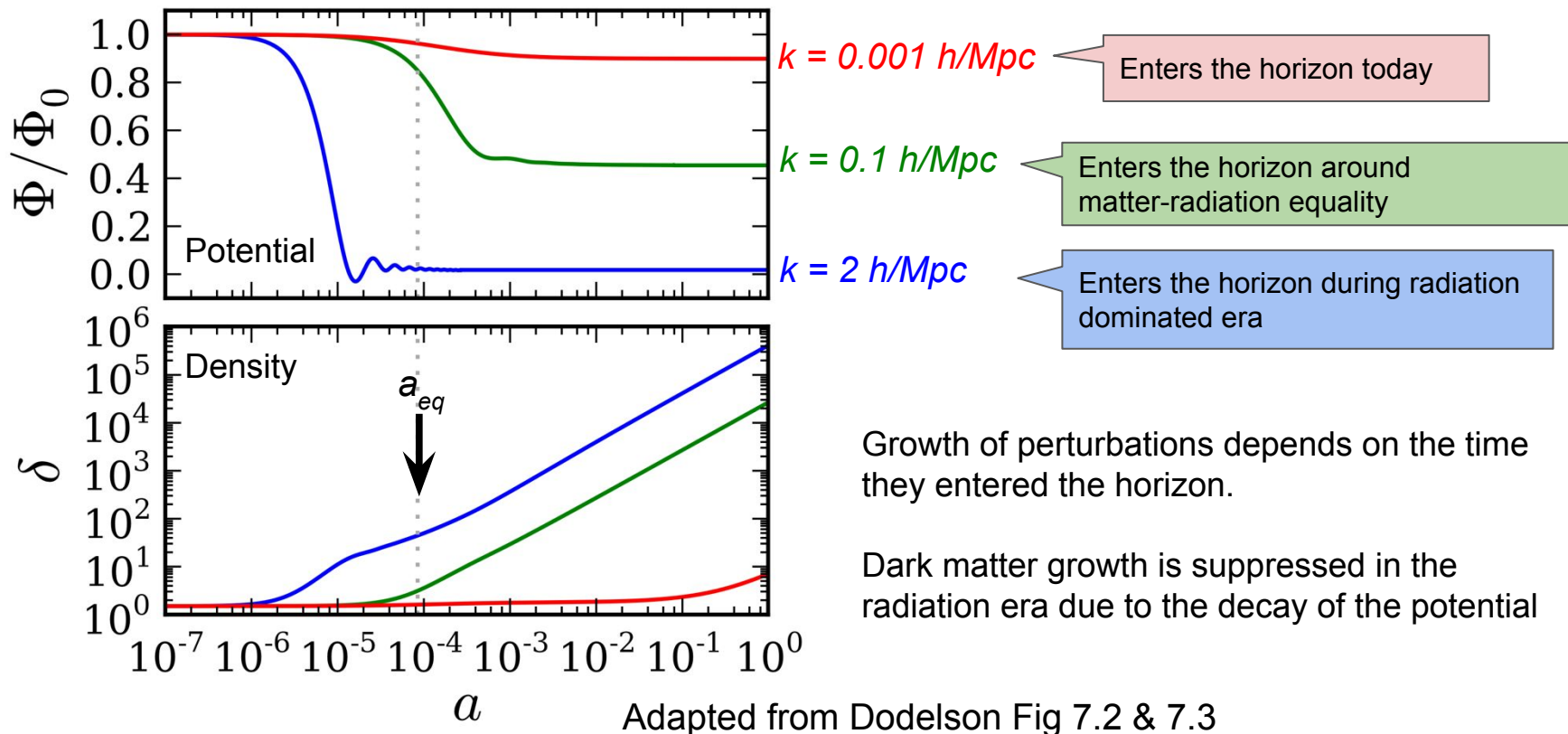
- In both cases with $\Omega=1$, the gravitational potential is constant in time.

Horizons

- On very large scales, density modes with wavelength larger than the light horizon size cannot collapse.



Evolution of density perturbations over cosmic time

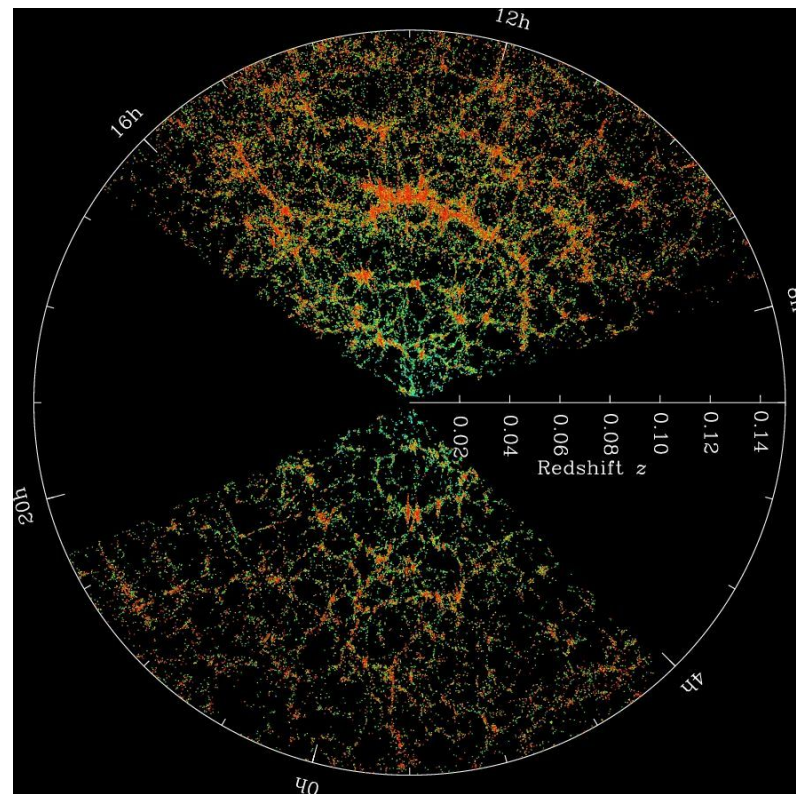


Summary

- Dynamical equations can be expanded in a series around the mean density. We use the first order expansion which is linear in density.
- We decomposed the density into Fourier waves. The Fourier modes evolve independently since equations are linear.
- The solution of the growth of density fluctuations depends on wavelength.
 - On large scales we find that the density grows proportional to the scale factor in a matter dominated universe (quadratically for radiation dominated epoch).
 - On small scales below the Jean's length, pressure counteracts collapse and acoustic waves travel. This happens in the dense plasma before recombination (cosmic microwave background).

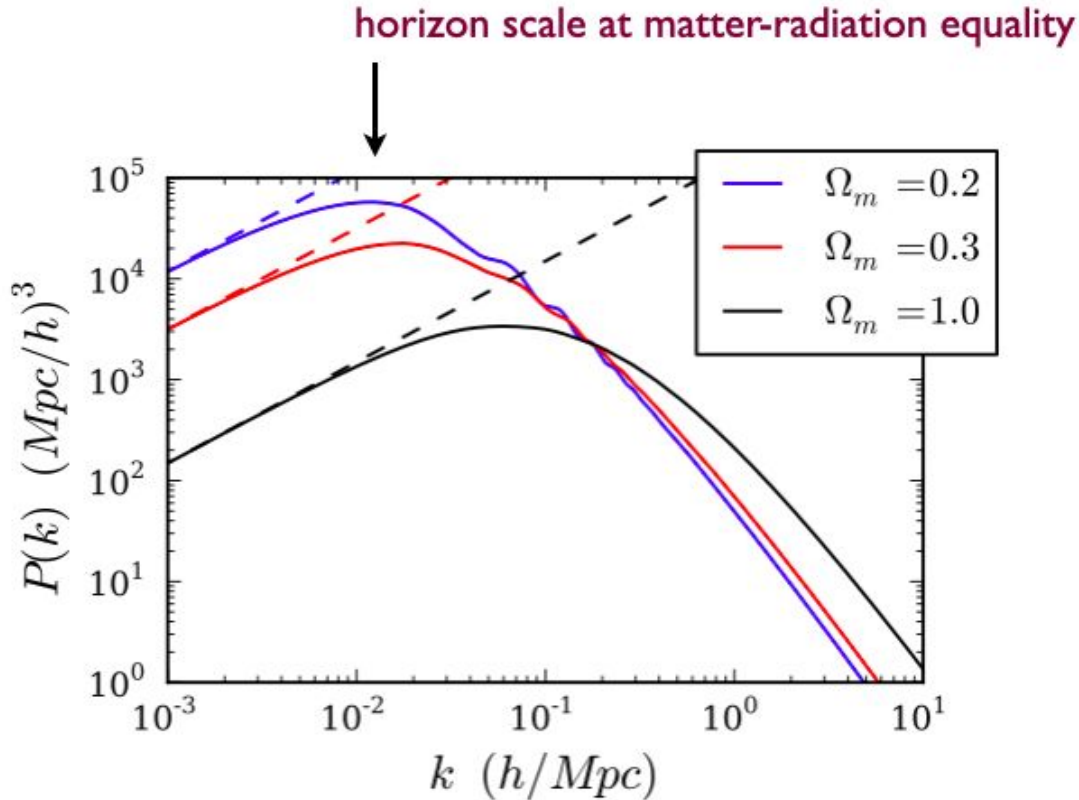
Galaxy redshift surveys

- Spectroscopic surveys measure the sky position of galaxies (RA , Dec) and redshift (z)
- Redshift gives a proxy for distance
- We use galaxies as tracers of the density field
- Relate perturbations in the galaxy field to perturbations in the density field with a bias factor.



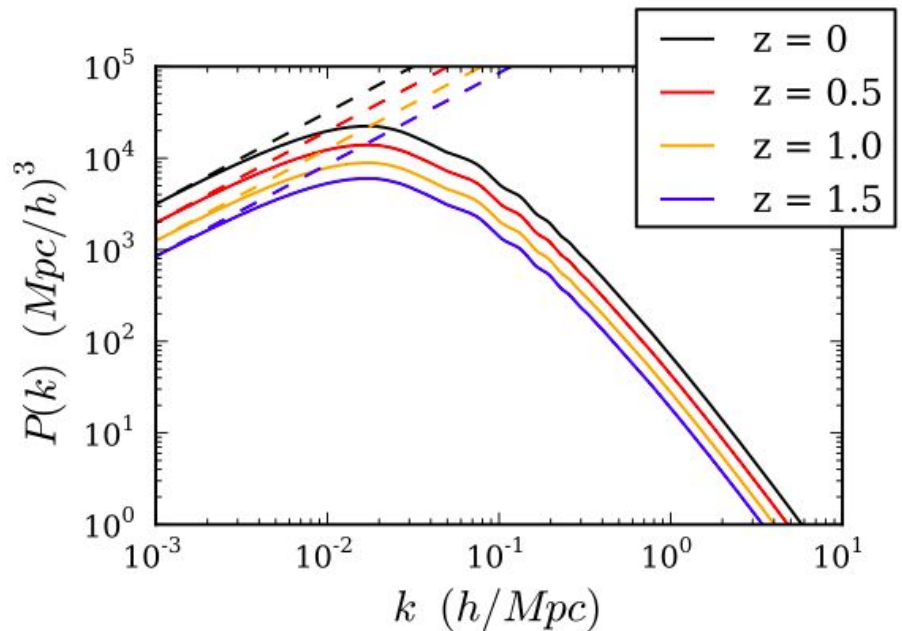
Sloan Digital Sky Survey (SDSS)

Shape of the power spectrum



- On very large scales ($k < 0.01$) the power spectrum follows the initial power spectrum established by inflation.
- The turnover corresponds to the horizon size at matter-radiation equality.
- Growth of small scales ($k > 0.1$) was suppressed since they were inside the horizon during the radiation epoch.

Evolution of the power spectrum



- The power spectrum grows with time according to the growth factor

$$\delta(z) = \delta(0)D(z)$$

- We also define σ_8 , the RMS of δ in a spherical window which evolves in the same way.

Fourier analysis

- Theory of structure formation is naturally formulated in Fourier space.
- Fourier modes evolve independently under gravity.
- The 3D over-density mode is

$$\delta_k(\vec{k}) = \int_{-\infty}^{\infty} \delta(\vec{r}) e^{-2\pi i \vec{k} \cdot \vec{r}} d^3\vec{r}$$

- The power spectrum is defined

$$P(\vec{k}) \equiv \langle |\delta_k(\vec{k})|^2 \rangle$$

Over-density is defined as

$$\delta(\vec{r}) = \frac{n(\vec{r}) - \bar{n}}{\bar{n}}$$

It can be computed by averaging over shells in k-space:

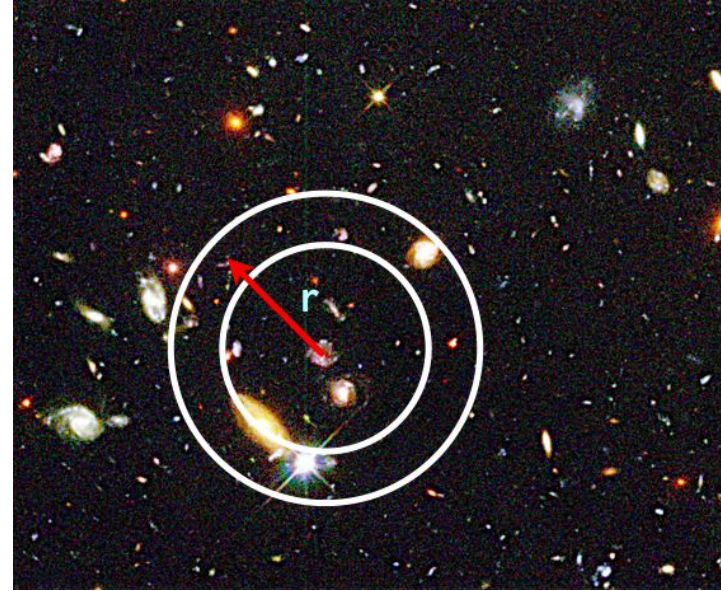
$$P(k) = \frac{1}{V} \sum_{|\vec{k}'|=k} |\delta_k(\vec{k}')|^2$$

Relation to the correlation function

- The correlation function characterises the distribution of pairs of galaxies
 - How many galaxies are expected in a spherical shell of radius r and width dr ?

$$dn(r) = \bar{n}(1 + \xi(r))4\pi r^2 dr$$

- The excess over a uniform distribution is given by the $1+\xi(r)$ term.
- $\xi=0$ for a uniform distribution.



The correlation function kernel

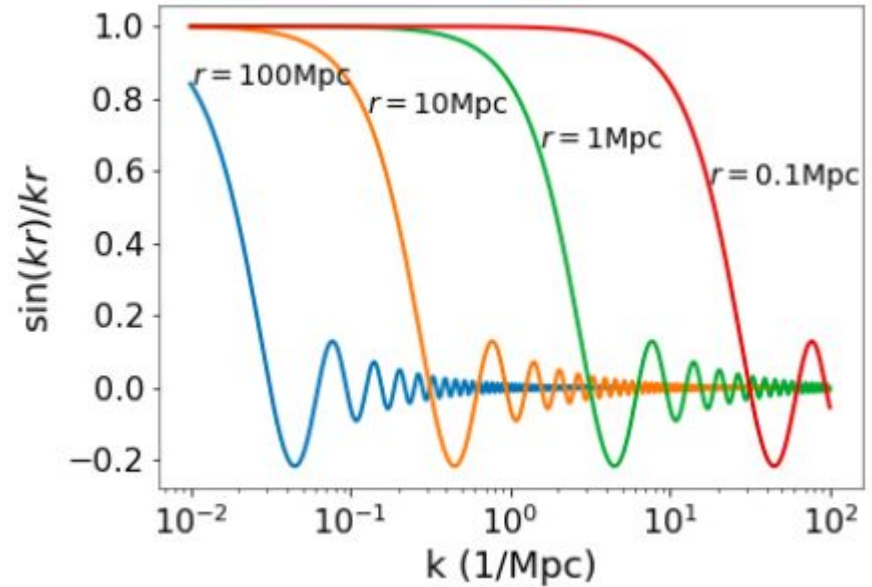
- The correlation function is the Fourier transform of the power spectrum

$$\xi(\vec{r}) = \frac{V}{(2\pi)^3} \int P(\vec{k}) e^{-i\vec{k} \cdot \vec{r}} d^3k$$

- If the field is isotropic, the angular part can be integrated to give

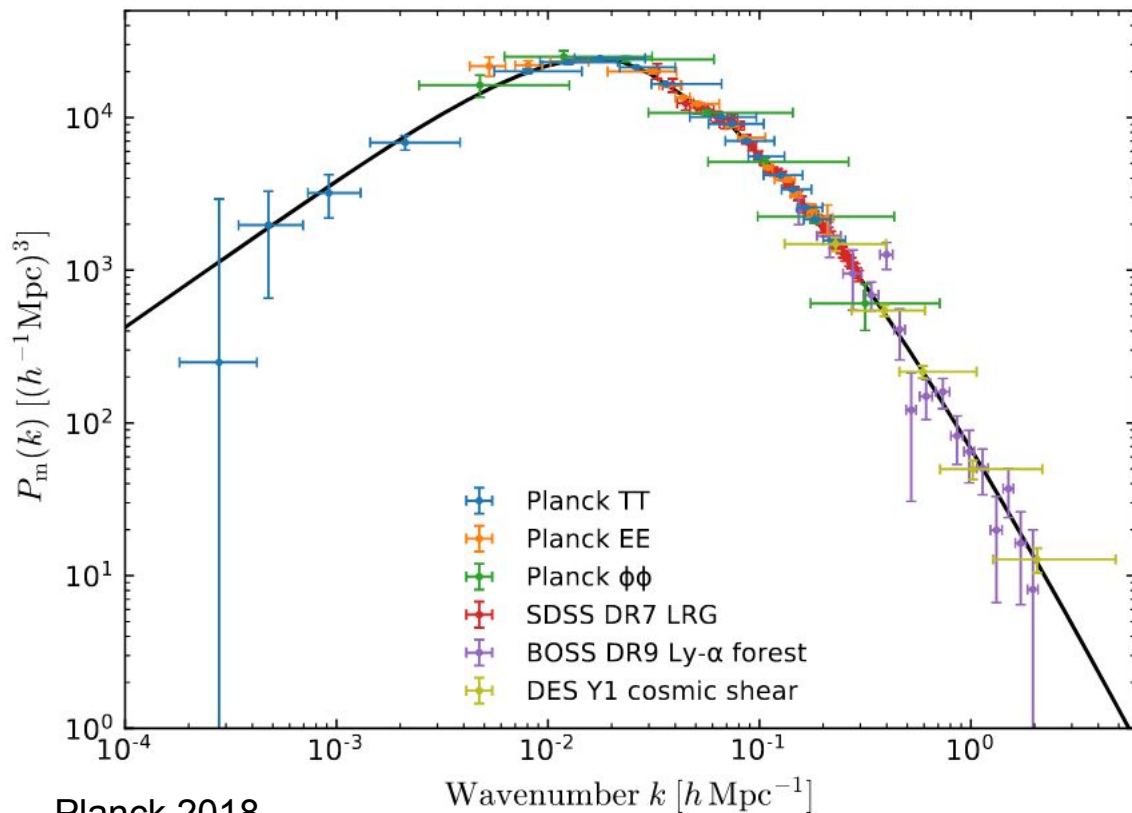
$$\xi(r) = \frac{V}{(2\pi)^3} \int P(k) \frac{\sin kr}{kr} 4\pi k^2 dk$$

- Fourier modes are mixed in the correlation function with the $\sin(kr)/kr$ kernel.



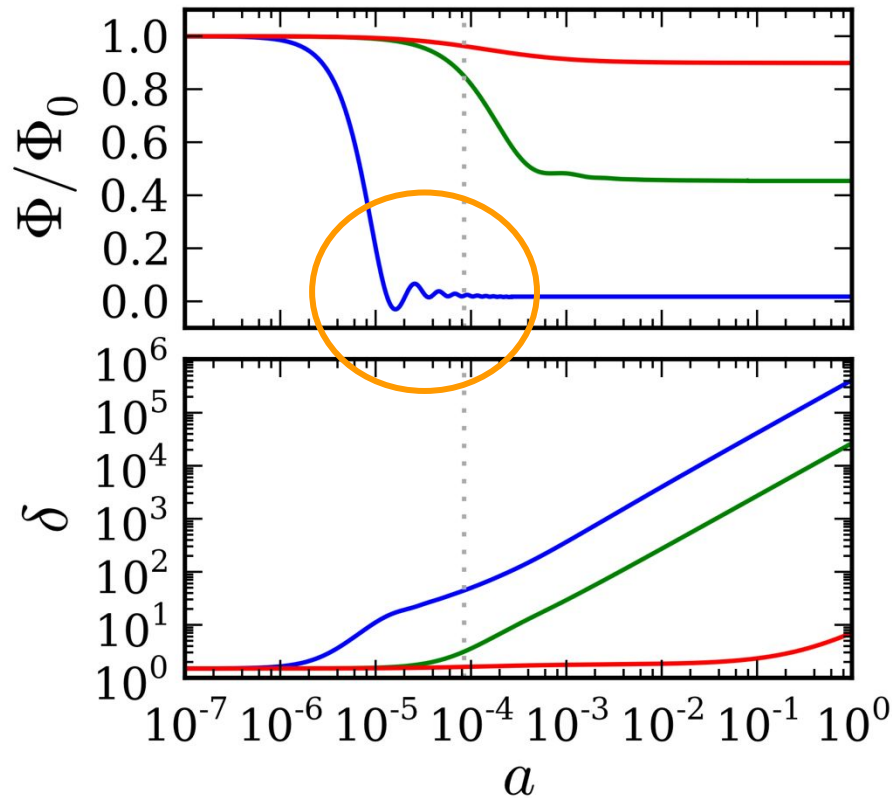
Cosmology with the matter power spectrum

- The shape depends on the matter density and baryon fraction.
- Neutrinos suppress power on small scales.
- Redshift-space distortions constrain the growth of structure and gravity model.
- Baryon acoustic oscillations give standard ruler to constrain the expansion history



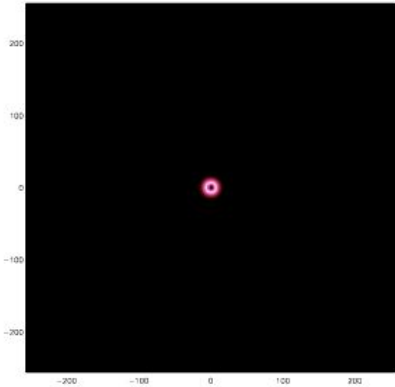
Baryon acoustic oscillations

- The pressure waves in the early Universe remain imprinted in the matter distribution after recombination (CMB)
- Enhancement of matter at separations of $\sim 100\text{Mpc}/h$ (sound horizon at recombination)
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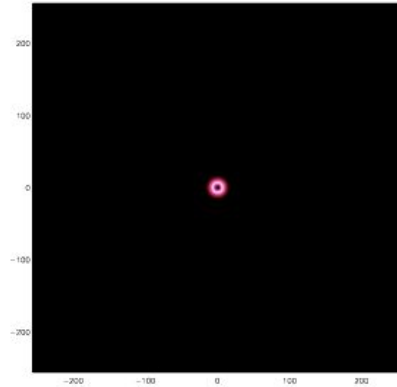


Acoustic oscillations

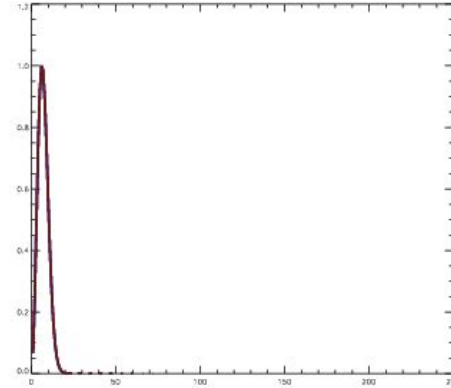
baryons



photons



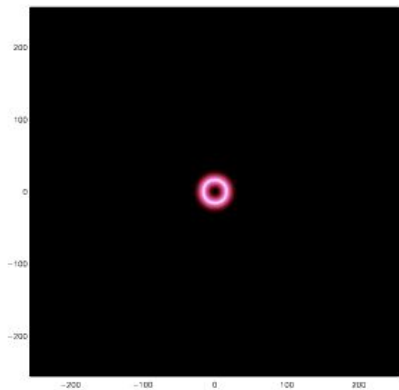
Mass profile



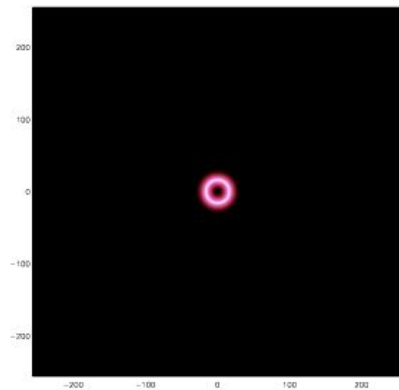
Consider an initially over-dense spot in the otherwise homogeneous Universe. Photons and baryons are tightly coupled and evolve together. The pressure pushes a shell out that continues to expand.

(Martin White, <http://w.astro.berkeley.edu/~mwhite/bao/>)

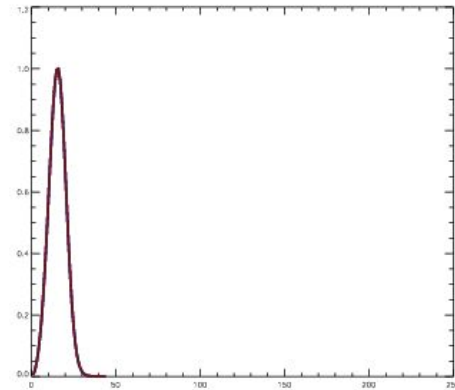
baryons



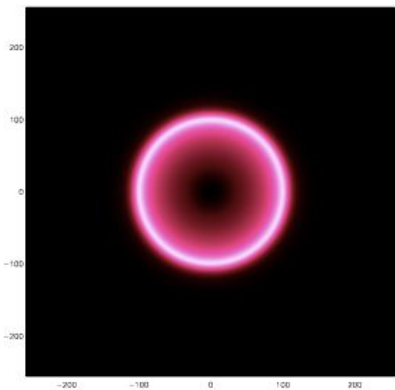
photons



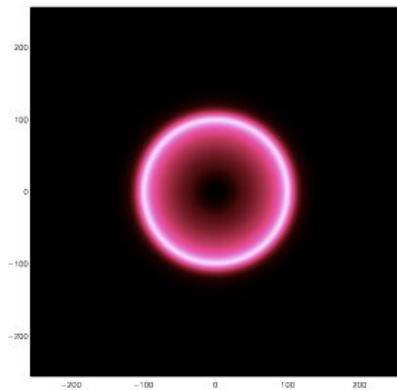
Mass profile



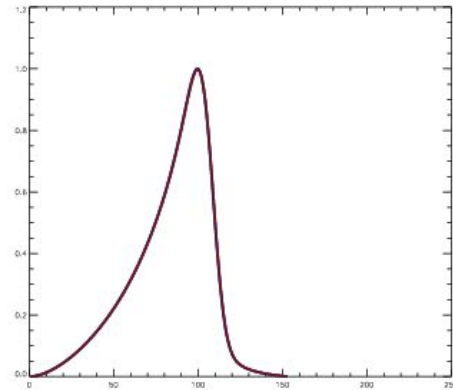
baryons



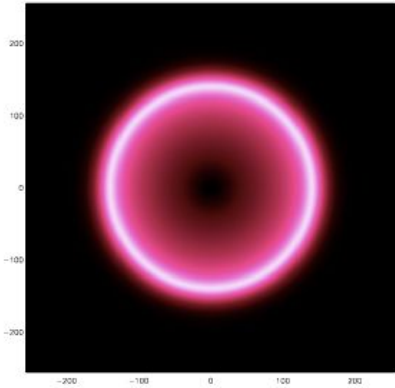
photons



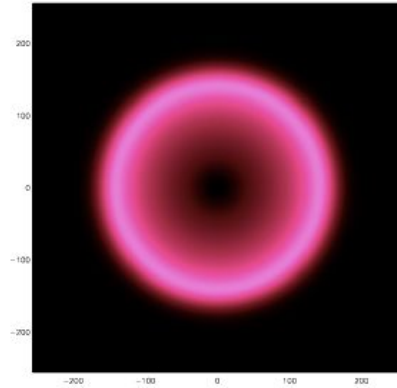
Mass profile



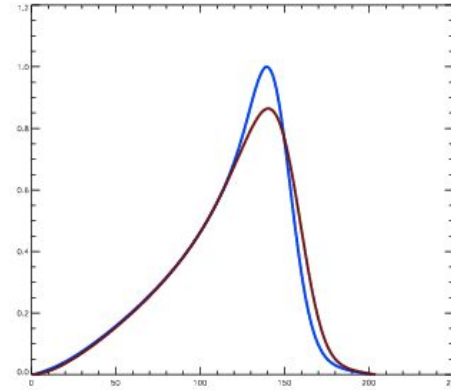
baryons



photons

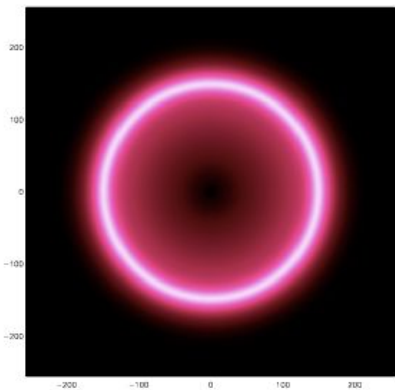


Mass profile

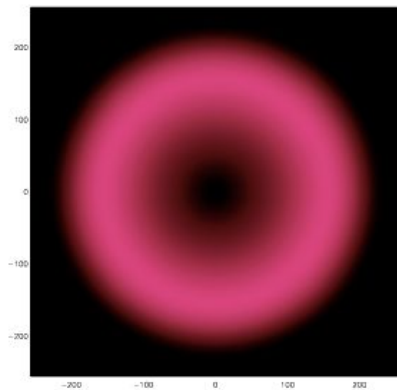


Recombination is starting $\sim 300\,000$ years after.
The photons are diffusing away from the matter density.

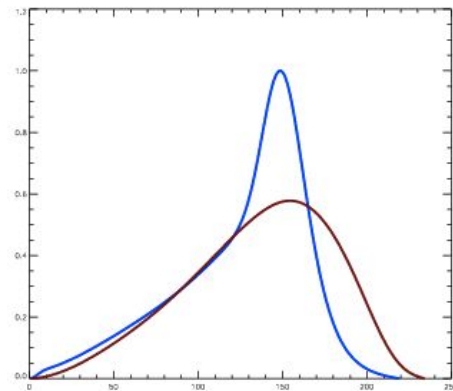
baryons



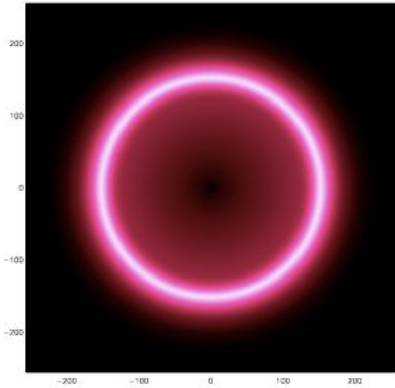
photons



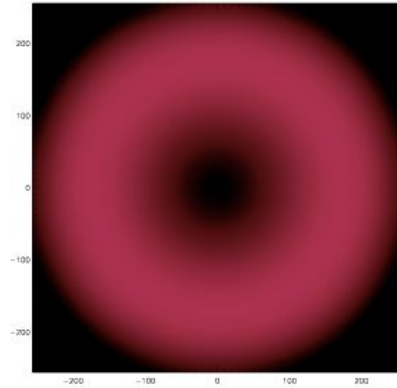
Mass profile



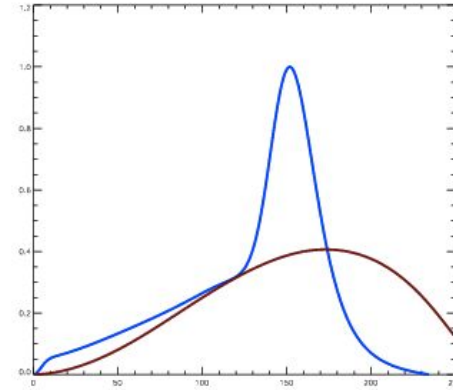
baryons



photons



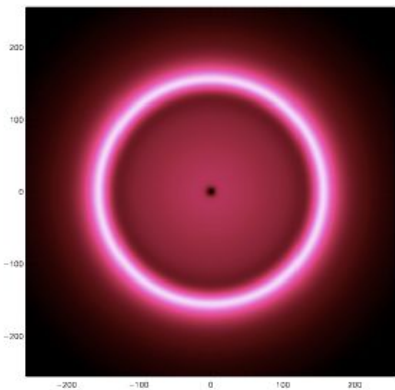
Mass profile



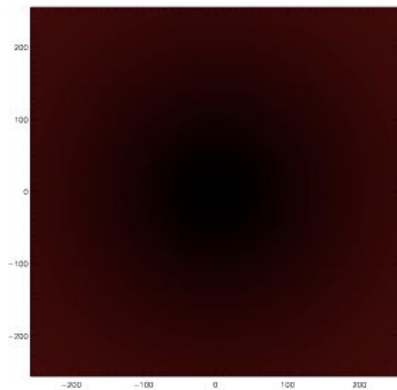
The photons are nearly homogeneous.

The dark matter over-density is growing under gravity

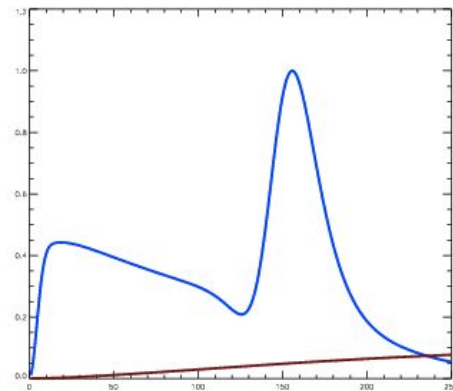
baryons



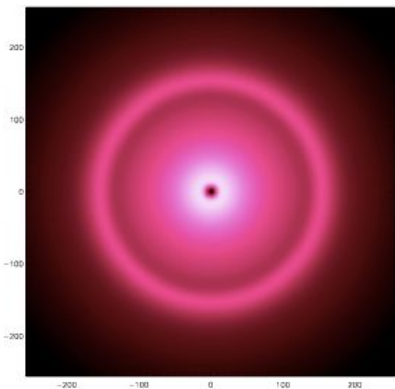
photons



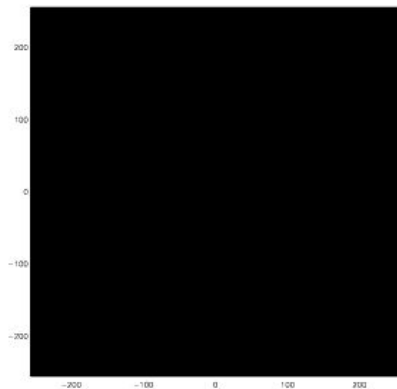
Mass profile



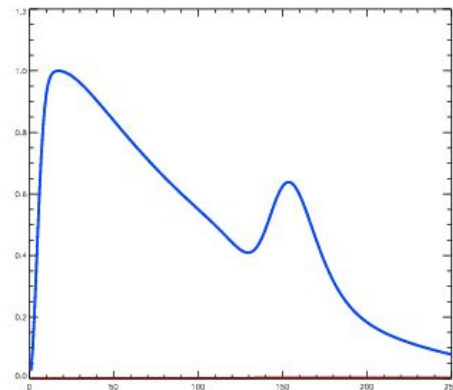
baryons



photons



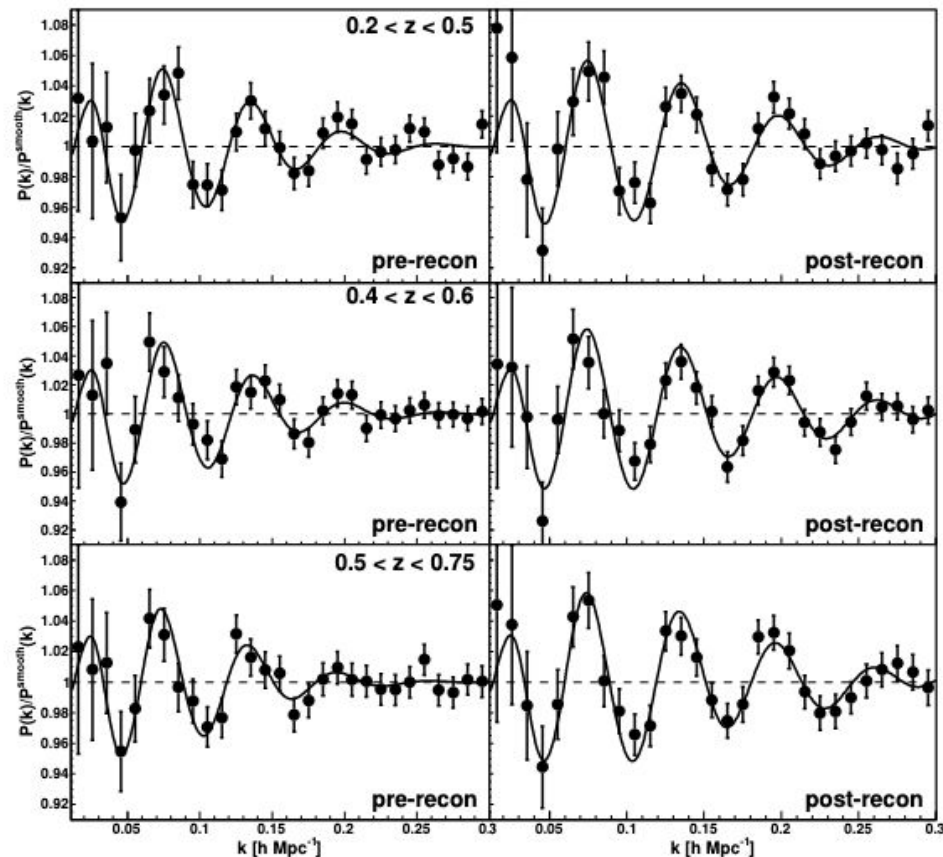
Mass profile



The end result is a peak in the matter profile at a scale of $\sim 100 \text{ Mpc/h}$.

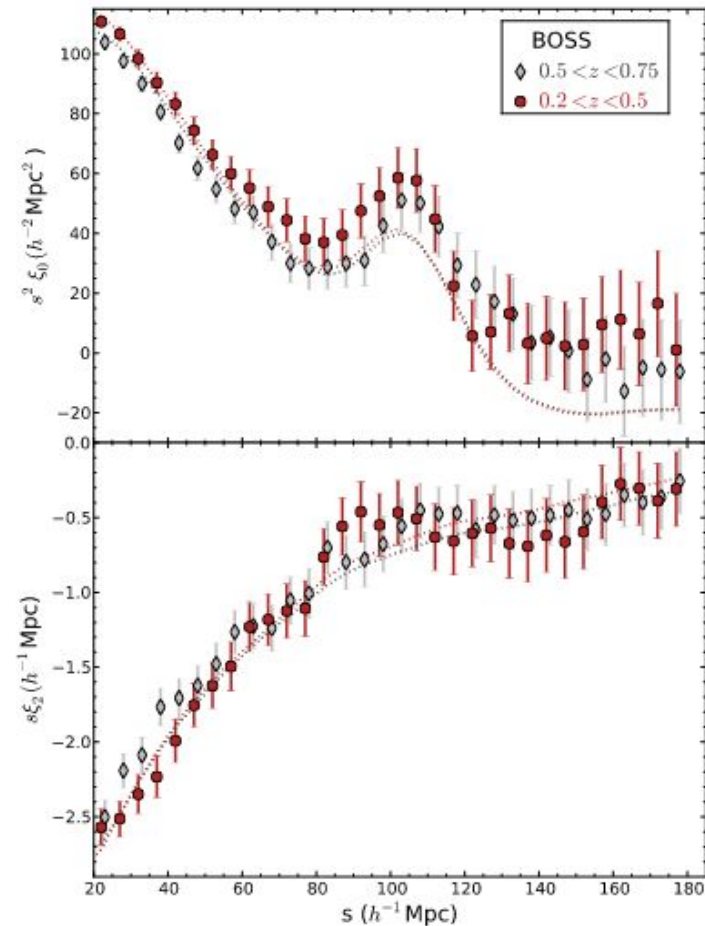
Baryon acoustic oscillations

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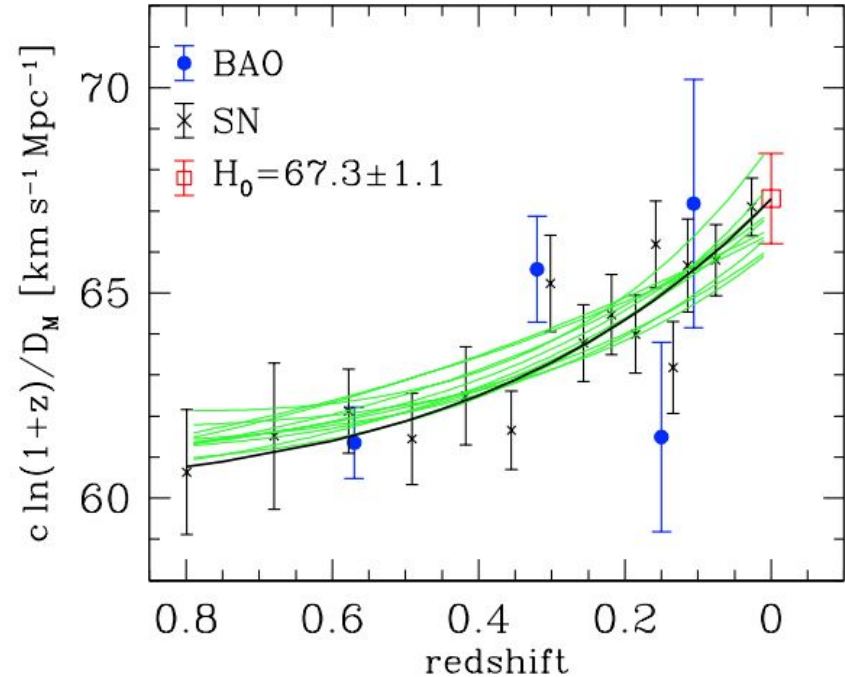
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Inverse distance ladder

- The BAO position gives a measure of the distance-redshift relation.
- BAO allows the distance ladder to be fixed at high redshift instead of with local cepheids (assuming a cosmological model).
- Supernovae distances may be calibrated against the BAO measures.
- Gives agreement with low $H_0 \sim 67$ km/s/Mpc (Aubourg+2015)
At tension with low redshift measures of H_0 .



Growth of structure and redshift-space distortions

- We saw the decomposition of the galaxy velocity into the Hubble flow plus a "peculiar velocity."
- The measured redshift has these two components.



$$z_{\text{measured}} = z_{\text{cosmo}} + (1 + z) v_{\text{peculiar}}/c$$

- The peculiar velocity is linked to the gravitational potential through the dynamical equations.

$$\delta v = \frac{2f}{3H\Omega} \nabla \delta \phi / a$$

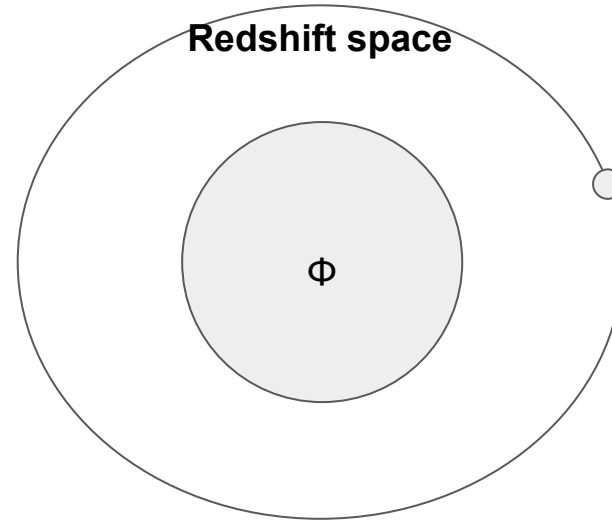
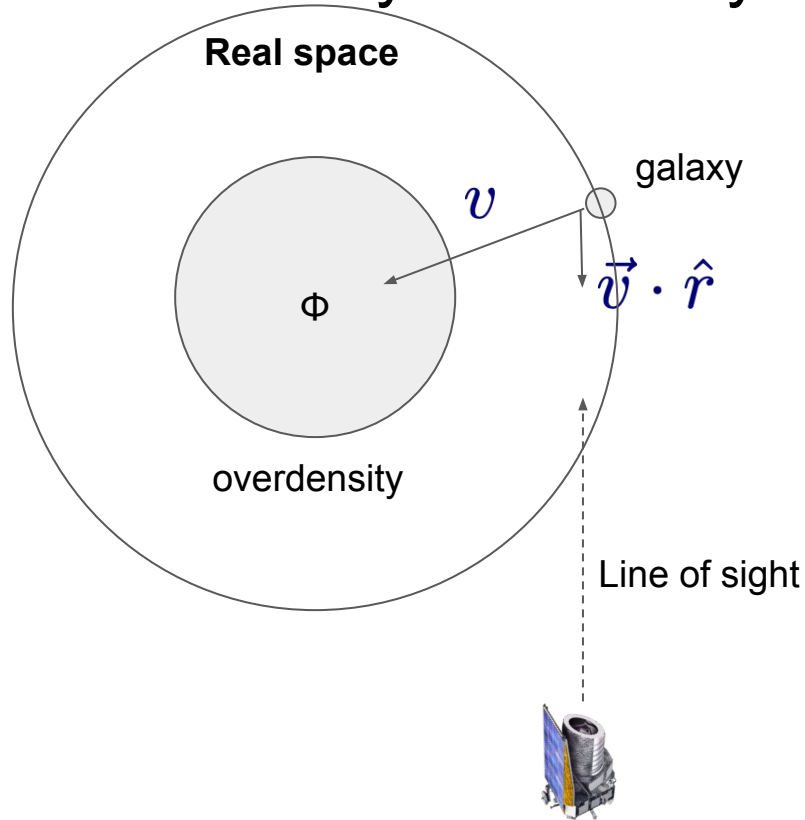
$$\vec{x}(t) = a(t)\vec{r}(t)$$

$$\vec{v} = \frac{d\vec{x}}{dt} = \frac{da}{dt}\vec{r} + a(t)\frac{d\vec{r}}{dt}$$

Hubble expansion   *Perturbation*

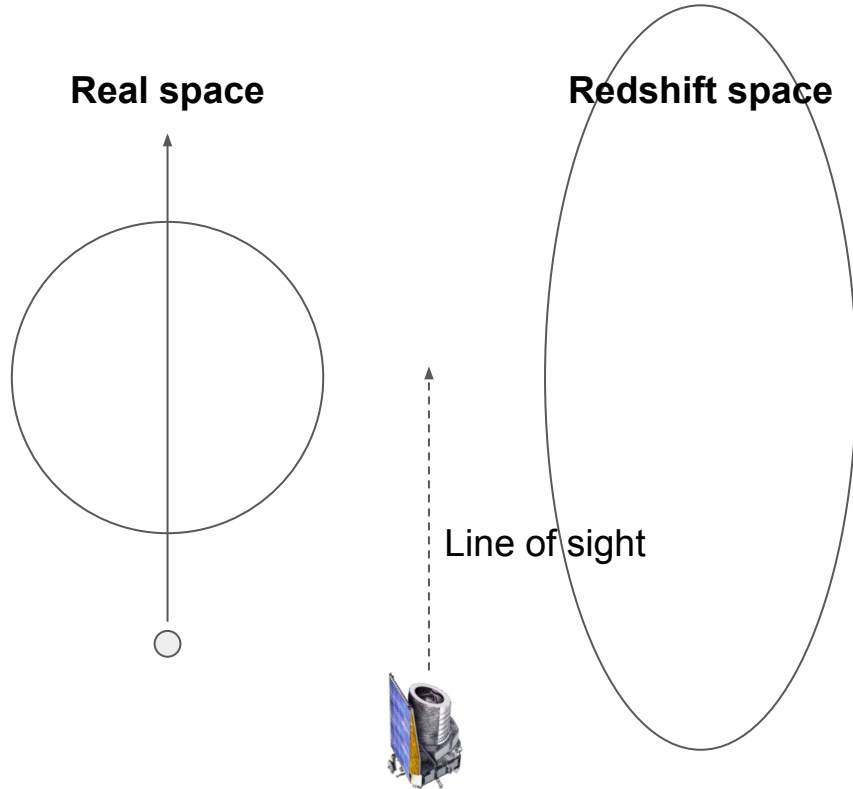
$$= H\vec{x} + \delta\vec{v}$$
$$\delta\vec{v}(t) = a(t)\vec{u}(t)$$

Galaxies systematically shift position in redshift space



- Galaxy motions towards overdensities leads to a systematic shift in redshift.
- A spherically symmetric distribution will appear squashed in redshift space.
- Known as the Kaiser effect (Kaiser 1987)

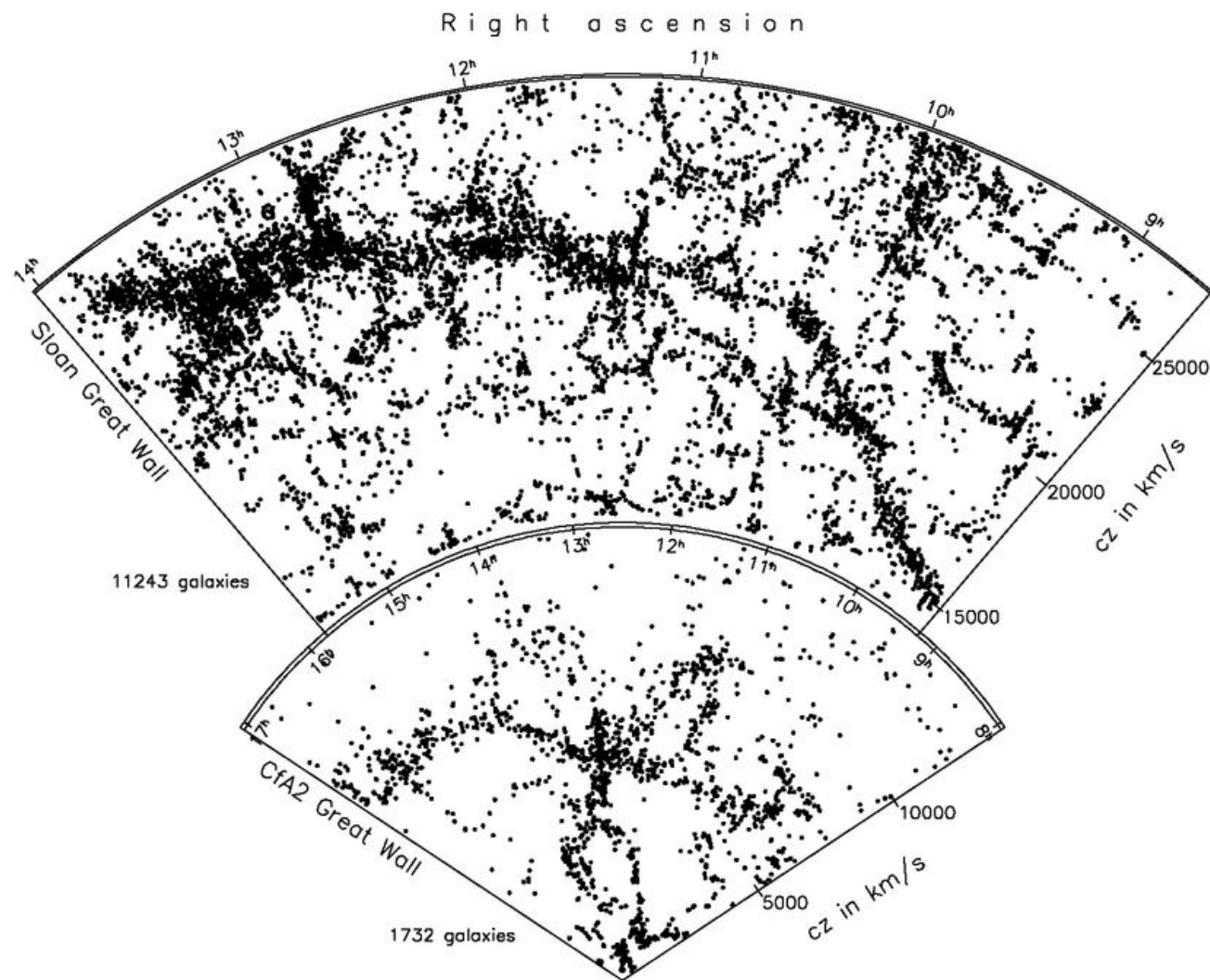
Fingers of God effect



- If the velocity is large, the shift in position in redshift space is large along the line of sight.
- Important in virialized galaxy cluster environments where galaxies are moving on orbits.
- A spherical cluster of galaxies will appear elongated along the line of sight.
- First reference: Jackson 1972

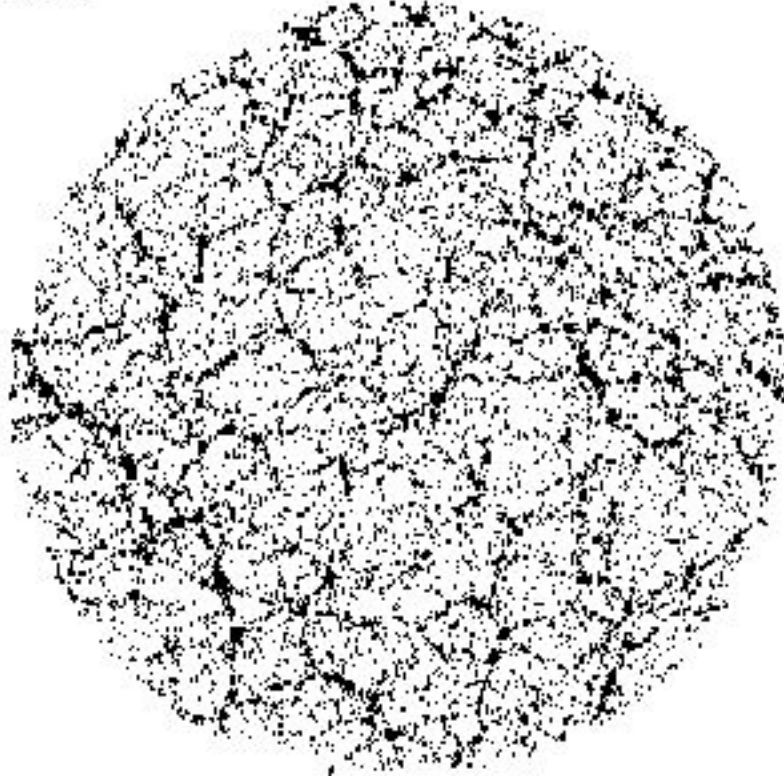
Redshift space distortions explain strange features seen in redshift survey maps.

- Dense filaments or walls across the line of sight.
- Elongated structures pointing radially.



Modifies the clustering signal

0.00

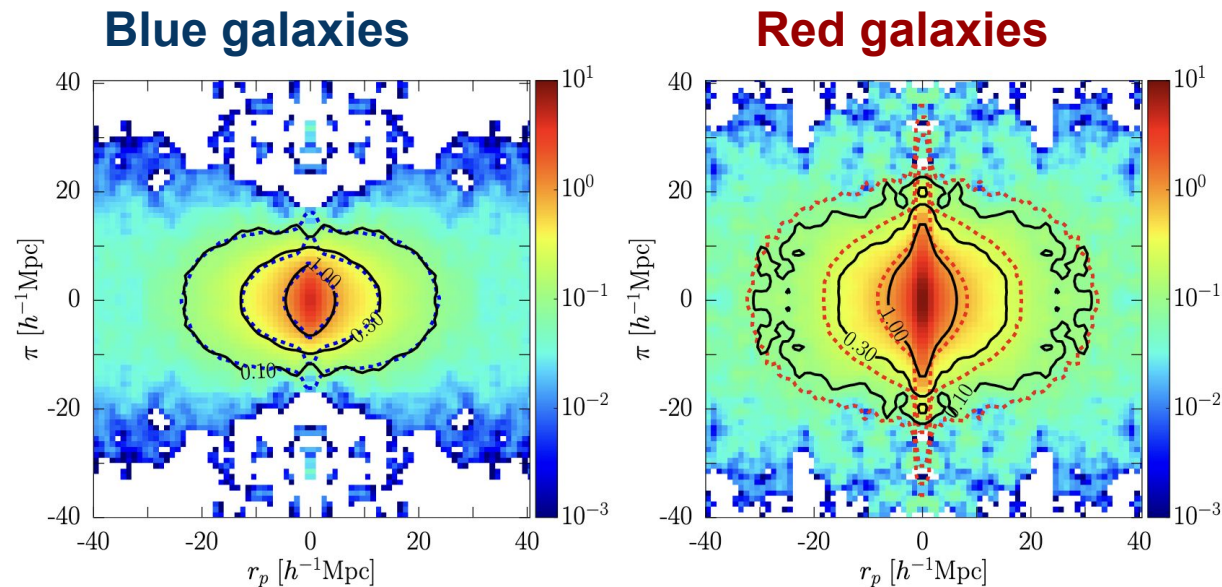


$$\delta v = \frac{2f}{3H\Omega} \nabla \delta \phi / a$$

In this animation the amplitude of line of sight velocities is varying.

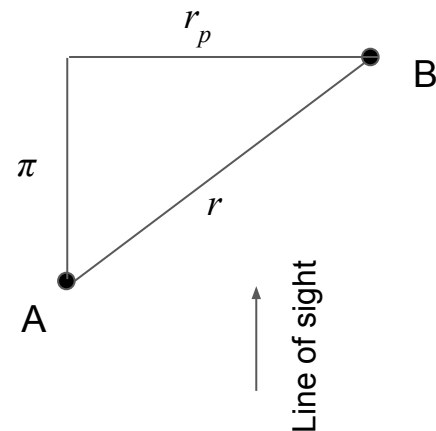
It shows both the large-scale squashing effect and radial Fingers.

Measurements of the correlation function



Two point correlation function measurements from VIPERS
(Mohammad+2018)

Red galaxies show a stronger "fingers of God" signal than blue star forming galaxies.



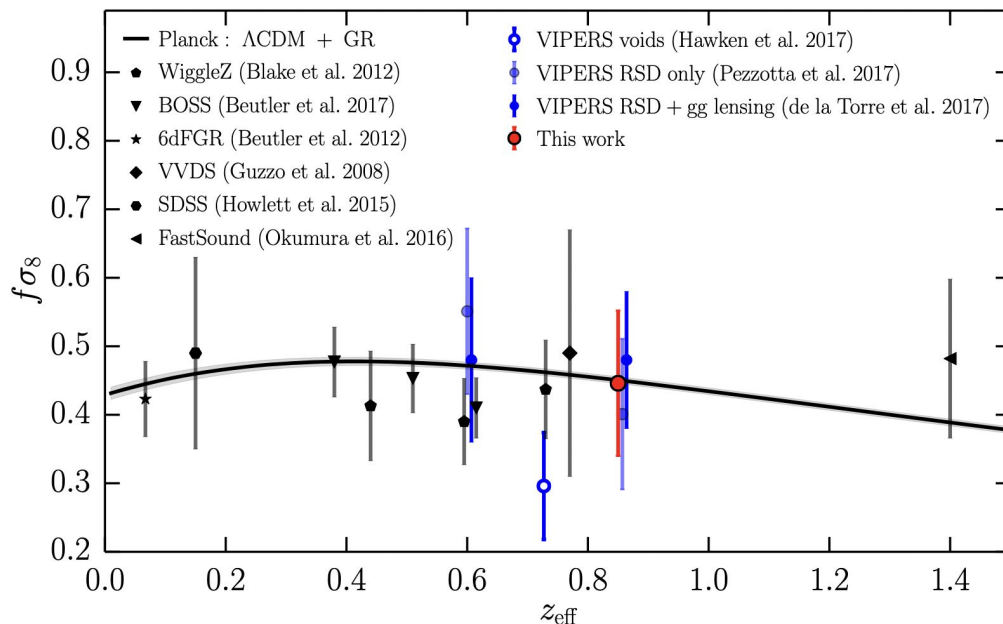
The correlation function binned in separation along and transverse to the line of sight.

The growth rate

- Fitting the anisotropic correlation function (or power spectrum) allows us to infer the parameter f .

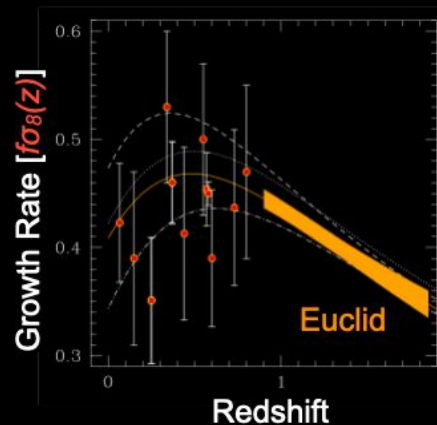
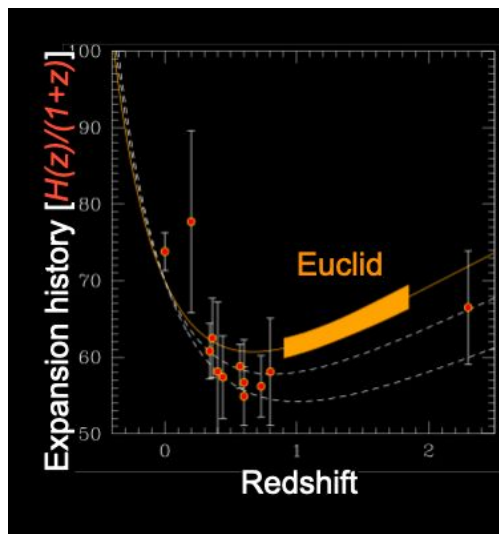
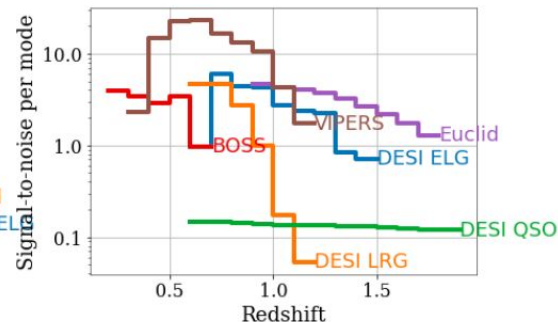
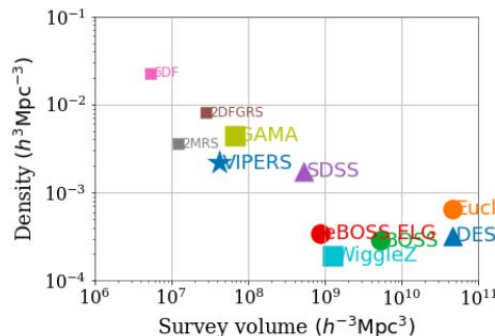
$$f = \frac{a}{\delta} \frac{d\delta}{da}$$
$$\approx \Omega_m(z)^\gamma$$

- The parameter gamma can be used to test General Relativity against alternative theories of gravity.

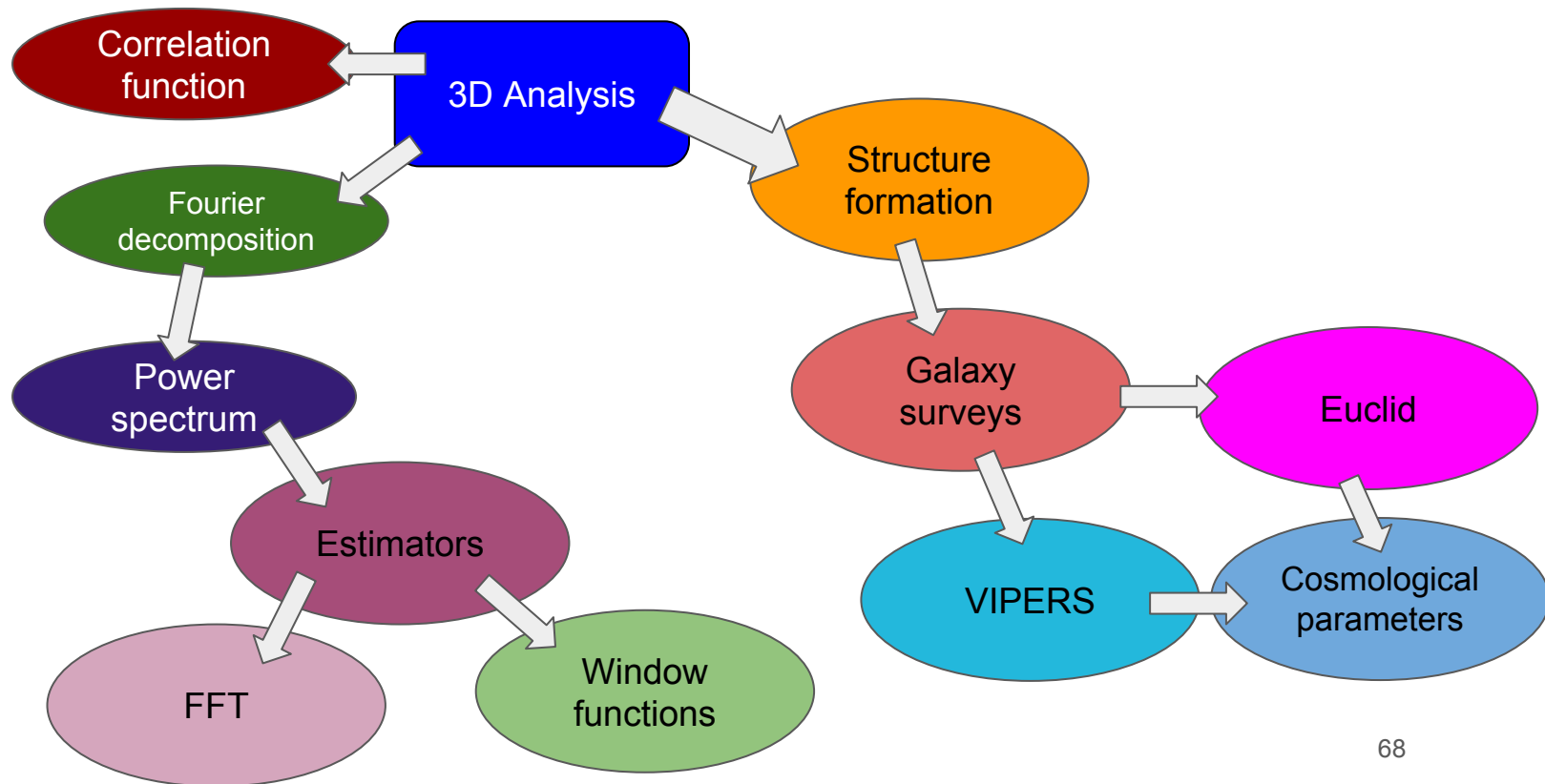


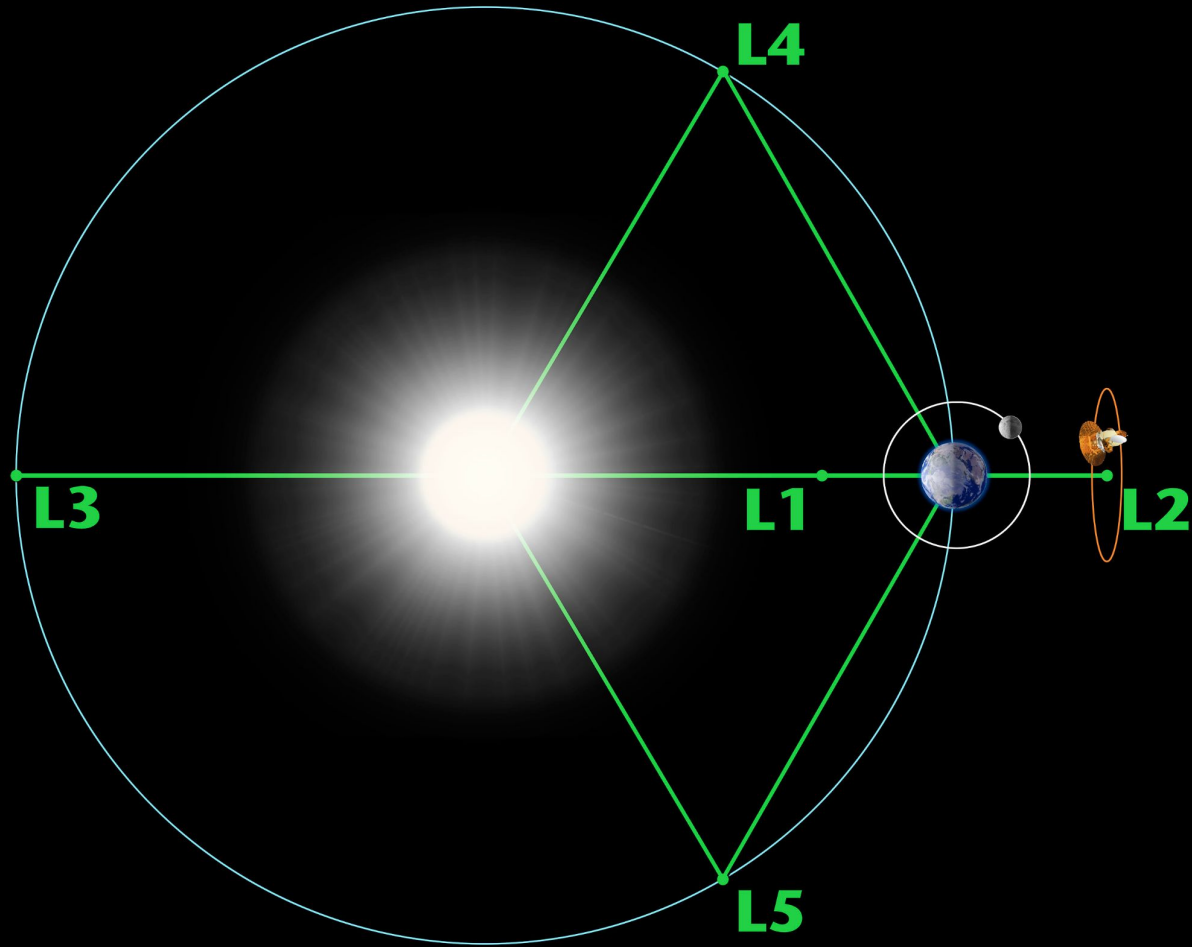
Forecasts

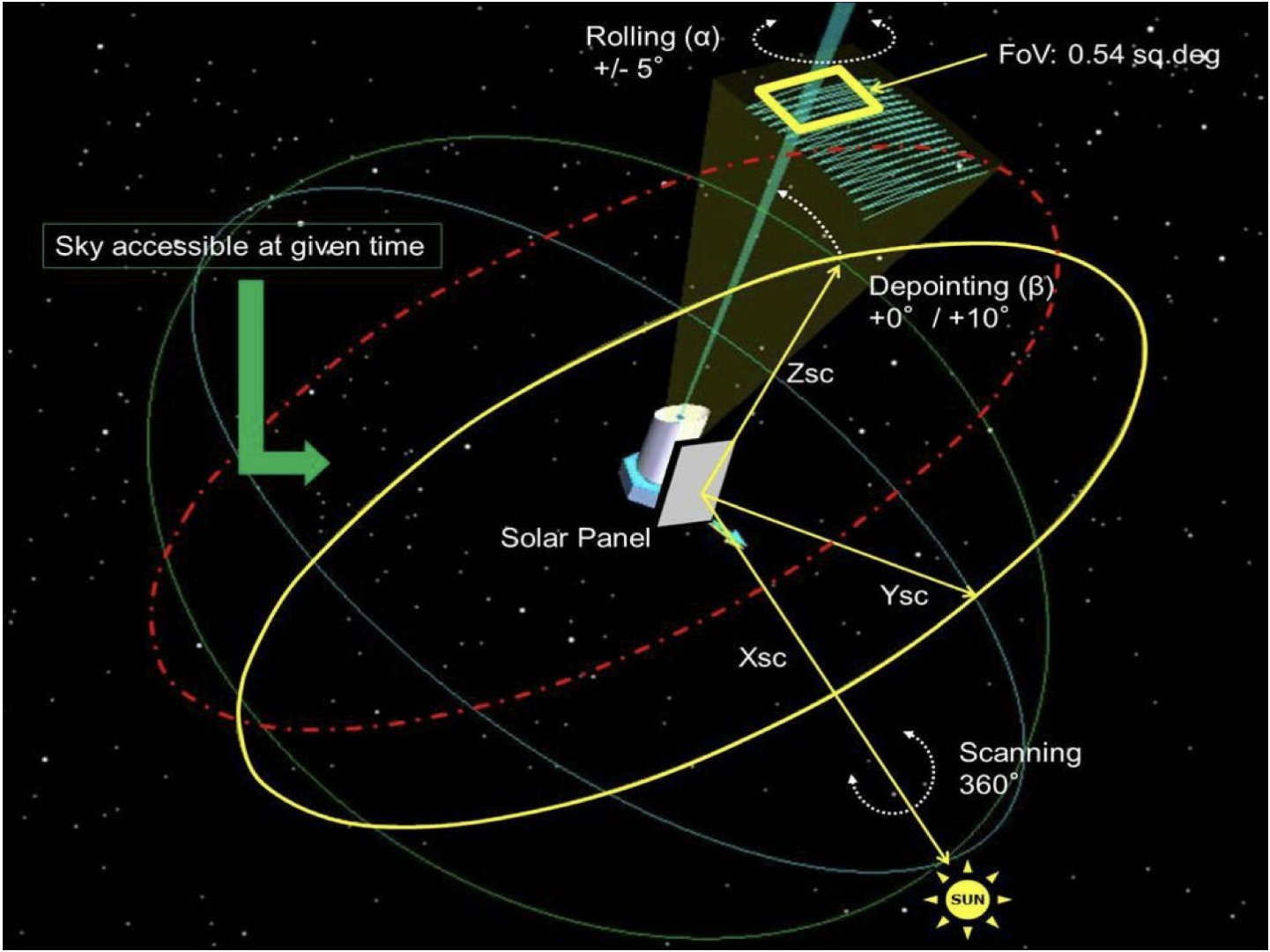
- Euclid spectroscopic galaxy power spectrum measurements will make percent-level constraints on the expansion history (BAO) and the growth rate (redshift-space distortions), as well as using full fits to the power spectrum/correlation function.
- The combined measurements from galaxy clustering, weak lensing and galaxy clusters can point us to new evidence for physics beyond the LambdaCDM model.



End of Chapter 3







Euclid survey and Euclid DR1 sky coverage

